## CHAPTER 6 THERMOCHEMISTRY: ENERGY FLOW AND CHEMICAL CHANGE

## END-OF-CHAPTER PROBLEMS

6.1 No, an increase in temperature means that heat has been transferred to the surroundings, which makes $q$ negative.
6.2 $\Delta E=q+w=w$, since $q=0$.

Thus, the change in work equals the change in internal energy.
6.3
a) electric heater
b) sound amplifier
c) light bulb
d) automobile alternator
6.4

| Heat energy; sound energy | (impact) |
| :--- | :--- |
| $\downarrow$ <br> Kinetic energy <br> $\downarrow$ | (falling text) |
| Potential energy |  |
| $\downarrow$ <br> Mechanical energy <br> $\downarrow$ <br> Chemical energy | (raised text) |
| (raising of text) |  |
| Che | (biological process to move muscles) |

6.5 Plan: The change in a system's energy is $\Delta E=q+w$. If the system receives heat, then its $q_{\text {final }}$ is greater than $q_{\text {initial }}$ so $q$ is positive. Since the system performs work, its $w_{\text {final }}<w_{\text {initial }}$ so $w$ is negative.
Solution:
$\Delta E=q+w$
$\Delta E=(+425 \mathrm{~J})+(-425 \mathrm{~J})=\mathbf{0} \mathbf{~ J}$
$6.6 \quad q+w=-255 \mathrm{cal}+(-428 \mathrm{cal})=\mathbf{6 8 3} \mathrm{cal}$
6.7 Plan: Convert $6.6 \times 10^{10} \mathrm{~J}$ to the other units using conversion factors.

Solution:
$\mathrm{C}(\mathrm{s})+\mathrm{O}_{2}(\mathrm{~g}) \rightarrow \mathrm{CO}_{2}(g)+6.6 \times 10^{10} \mathrm{~J}$
(2.0 tons)
a) $\Delta E(\mathrm{~kJ})=\left(6.6 \times 10^{10} \mathrm{~J}\right)\left(\frac{1 \mathrm{~kJ}}{10^{3} \mathrm{~J}}\right)=\mathbf{6 . 6 \times 1 0} \mathbf{0}^{7} \mathbf{~ k J}$
b) $\Delta E(\mathrm{kcal})=\left(6.6 \times 10^{10} \mathrm{~J}\right)\left(\frac{1 \mathrm{cal}}{4.184 \mathrm{~J}}\right)\left(\frac{1 \mathrm{kcal}}{10^{3} \mathrm{cal}}\right)=1.577 \times 10^{7}=\mathbf{1 . 6 \times 1 0 ^ { 7 }} \mathbf{~ k c a l}$
c) $\Delta E(\mathrm{Btu})=\left(6.6 \times 10^{10} \mathrm{~J}\right)\left(\frac{1 \mathrm{Btu}}{1055 \mathrm{~J}}\right)=6.256 \times 10^{7}=\mathbf{6 . 3 \times 1 0}{ }^{7} \mathbf{B t u}$
$6.8 \quad \mathrm{CaCO}_{3}(\mathrm{~s})+9.0 \times 10^{6} \mathrm{~kJ} \rightarrow \mathrm{CaO}(\mathrm{s})+\mathrm{CO}_{2}(\mathrm{~g})$ (5.0 tons)
a) $\Delta E(\mathrm{~J})=\left(9.0 \times 10^{6} \mathrm{~kJ}\right)\left(\frac{10^{3} \mathrm{~J}}{1 \mathrm{~kJ}}\right)=\mathbf{9 . 0 \times 1 0} \mathbf{9}^{\mathbf{~}} \mathbf{J}$
b) $\Delta E(\mathrm{cal})=\left(9.0 \times 10^{6} \mathrm{~kJ}\right)\left(\frac{10^{3} \mathrm{~J}}{1 \mathrm{~kJ}}\right)\left(\frac{1 \mathrm{cal}}{4.184 \mathrm{~J}}\right)=2.15105 \times 10^{9}=2.2 \times 10^{9} \mathrm{cal}$
c) $\Delta E(\mathrm{Btu})=\left(9.0 \times 10^{6} \mathrm{~kJ}\right)\left(\frac{10^{3} \mathrm{~J}}{1 \mathrm{~kJ}}\right)\left(\frac{1 \mathrm{Btu}}{1055 \mathrm{~J}}\right)=8.5308 \times 10^{6}=\mathbf{8 . 5 \times 1 0 ^ { 6 }} \mathbf{B t u}$

$$
\begin{aligned}
& \Delta E(\mathrm{~J})=\left(4.1 \times 10^{3} \text { Calorie }\right)\left(\frac{10^{3} \mathrm{cal}}{1 \text { Calorie }}\right)\left(\frac{4.184 \mathrm{~J}}{1 \mathrm{cal}}\right)=1.7154 \times 10^{7}=\mathbf{1 . 7 \times 1 0 ^ { 7 }} \mathbf{~ J} \\
& \Delta E(\mathrm{~kJ})=\left(4.1 \times 10^{3} \text { Calorie }\right)\left(\frac{10^{3} \mathrm{cal}}{1 \text { Calorie }}\right)\left(\frac{4.184 \mathrm{~J}}{1 \mathrm{cal}}\right)\left(\frac{1 \mathrm{~kJ}}{10^{3} \mathrm{~J}}\right)=1.7154 \times 10^{4}=\mathbf{1 . 7 \times 1 0 ^ { 4 }} \mathbf{~ k J}
\end{aligned}
$$

6.10 Plan: An exothermic process releases heat and an endothermic process absorbs heat.

Solution:
a) Exothermic, the system (water) is releasing heat in changing from liquid to solid.
b) Endothermic, the system (water) is absorbing heat in changing from liquid to gas.
c) Exothermic, the process of digestion breaks down food and releases energy.
d) Exothermic, heat is released as a person runs and muscles perform work.
e) Endothermic, heat is absorbed as food calories are converted to body tissue.
f) Endothermic, the wood being chopped absorbs heat (and work).
g) Exothermic, the furnace releases heat from fuel combustion. Alternatively, if the system is defined as the air in the house, the change is endothermic since the air's temperature is increasing by the input of heat energy from the furnace.
6.11 Absolute enthalpy values, like absolute energy values, are unknown.
6.12 Plan: An exothermic reaction releases heat, so the reactants have greater $H\left(H_{\text {initial }}\right)$ than the products $\left(H_{\text {final }}\right)$. $\Delta H=H_{\text {final }}-H_{\text {initial }}<0$.
Solution:


6.14 Plan: Combustion of hydrocarbons and related compounds require oxygen (and a heat catalyst) to yield carbon dioxide gas, water vapor, and heat. Combustion reactions are exothermic. The freezing of liquid water is an exothermic process as heat is removed from the water in the conversion from liquid to solid. An exothermic reaction or process releases heat, so the reactants have greater $H\left(H_{\text {initial }}\right)$ than the products ( $H_{\text {final }}$ ).

Solution:
a) Combustion of ethane: $2 \mathrm{C}_{2} \mathrm{H}_{6}(\mathrm{~g})+7 \mathrm{O}_{2}(\mathrm{~g}) \rightarrow 4 \mathrm{CO}_{2}(\mathrm{~g})+6 \mathrm{H}_{2} \mathrm{O}(\mathrm{g})+$ heat

b) Freezing of water: $\mathrm{H}_{2} \mathrm{O}(\mathrm{l}) \rightarrow \mathrm{H}_{2} \mathrm{O}(\mathrm{s})+$ heat

$$
\underline{\mathrm{H}_{2} \mathrm{O}(l) \text { (initial) }}
$$


a) $\mathrm{Na}(\mathrm{s})+1 / 2 \mathrm{Cl}_{2}(g) \rightarrow \mathrm{NaCl}(s)+$ heat
$\underline{\mathrm{Na}(\mathrm{s})+1 / 2 \mathrm{Cl}_{2}(g)}$

b) $\mathrm{C}_{6} \mathrm{H}_{6}(\mathrm{l})+$ heat $\rightarrow \mathrm{C}_{6} \mathrm{H}_{6}(\mathrm{~g})$
$\mathrm{C}_{6} \mathrm{H}_{6}(g)$

6.16 Plan: Combustion of hydrocarbons and related compounds require oxygen (and a heat catalyst) to yield carbon dioxide gas, water vapor, and heat. Combustion reactions are exothermic. An exothermic reaction releases heat, so the reactants have greater $H\left(H_{\text {initial }}\right)$ than the products ( $\left.H_{\text {final }}\right)$. If heat is absorbed, the reaction is endothermic and the products have greater $H\left(H_{\text {final }}\right)$ than the reactants $\left(H_{\text {initial }}\right)$.
Solution:
a) $2 \mathrm{CH}_{3} \mathrm{OH}(\mathrm{l})+3 \mathrm{O}_{2}(\mathrm{~g}) \rightarrow 2 \mathrm{CO}_{2}(\mathrm{~g})+4 \mathrm{H}_{2} \mathrm{O}(g)+$ heat $\underline{2 \mathrm{CH}_{3} \mathrm{OH}+3 \mathrm{O}_{2} \text { (initial) }}$

b) Nitrogen dioxide, $\mathrm{NO}_{2}$, forms from $\mathrm{N}_{2}$ and $\mathrm{O}_{2}$.

a) $\mathrm{CO}_{2}(\mathrm{~s})+$ heat $\rightarrow \mathrm{CO}_{2}(\mathrm{~g})$

$\Delta H=(+),($ endothermic $)$
b) $\mathrm{SO}_{2}(g)+1 / 2 \mathrm{O}_{2}(g) \rightarrow \mathrm{SO}_{3}(g)+$ heat

6.18 Plan: Recall that $q_{\text {sys }}$ is positive if heat is absorbed by the system (endothermic) and negative if heat is released by the system (exothermic). Since $\Delta E=q+w$, the work must be considered in addition to $q_{\text {sys }}$ to find $\Delta E_{\text {sys }}$. Solution:
a) This is a phase change from the solid phase to the gas phase. Heat is absorbed by the system so $q_{\text {sys }}$ is positive (+).
b) The system is expanding in volume as more moles of gas exist after the phase change than were present before the phase change. So the system has done work of expansion and $w$ is negative. $\Delta E_{\text {sys }}=q+w$. Since $q$ is positive and $w$ is negative, the sign of $\Delta E_{\text {sys }}$ cannot be predicted. It will be positive if $q>w$ and negative if $q<w$.
c) $\Delta E_{\text {univ }}=\mathbf{0}$. If the system loses energy, the surroundings gain an equal amount of energy. The sum of the energy of the system and the energy of the surroundings remains constant.
6.19 a) There is a volume decrease; $V_{\text {final }}<V_{\text {initial }}$ so $\Delta V$ is negative. Since $w_{\text {sys }}=-P \Delta V$, $w$ is positive, + . b) $\Delta H_{\text {sys }}$ is - as heat has been removed from the system to liquefy the gas.
c) $\Delta E_{\text {sys }}=q+w$. Since $q$ is negative and $w$ is positive, the sign of $\Delta E_{\text {sys }}$ and $\Delta E_{\text {surr }}$ cannot be predicted. $\Delta E_{\text {sys }}$ will be positive and $\Delta E_{\text {surr }}$ will be negative if $w>q$ and $\Delta E_{\text {sys }}$ will be negative and $\Delta E_{\text {surr }}$ will be positive if $w<q$.
6.20 To determine the specific heat capacity of a substance, you need its mass, the heat added (or lost), and the change in temperature.
6.21 Specific heat capacity is an intensive property; it is defined on a per gram basis. The specific heat capacity of a particular substance has the same value, regardless of the amount of substance present.

Plan: The heat required to raise the temperature of water is found by using the equation $q=c \times$ mass $\times \Delta T$. The specific heat capacity, $c_{\text {water }}$, is found in Table 6.2. Because the Celsius degree is the same size as the Kelvin degree, $\Delta T=100^{\circ} \mathrm{C}-25^{\circ} \mathrm{C}=75^{\circ} \mathrm{C}=75 \mathrm{~K}$.
Solution:
$q(\mathrm{~J})=c \times$ mass $\times \Delta T=\left(4.184 \frac{\mathrm{~J}}{\mathrm{~g} \cdot \mathrm{~K}}\right)(22.0 \mathrm{~g})(75 \mathrm{~K})=6903.6=\mathbf{6 . 9 \times 1 0 ^ { 3 }} \mathbf{J}$
$q(\mathrm{~J})=c \times \operatorname{mass} \mathrm{x} \Delta T=\left(2.087 \frac{\mathrm{~J}}{\mathrm{~g} \cdot \mathrm{~K}}\right)(0.10 \mathrm{~g})((-75-10) \mathrm{K})=-17.7395=.\mathbf{- 1 8} \mathbf{~ J}$

Plan: Use the relationship $q=c \times$ mass $\mathrm{x} \Delta T$. We know the heat (change kJ to J ), the specific heat capacity, and the mass, so $\Delta T$ can be calculated. Once $\Delta T$ is known, that value is added to the initial temperature to find the final temperature.
Solution:

$$
\begin{aligned}
& q(\mathrm{~J})=c \times \text { mass } \times \Delta T \quad T_{\text {initial }}=13.00^{\circ} \mathrm{C} \quad T_{\text {final }}=? \quad \text { mass }=295 \mathrm{~g} \quad c=0.900 \mathrm{~J} / \mathrm{g} \cdot \mathrm{~K} \\
& q=(75.0 \mathrm{~kJ})\left(\frac{10^{3} \mathrm{~J}}{1 \mathrm{~kJ}}\right)=7.50 \times 10^{4} \mathrm{~J} \\
& 7.50 \times 10^{4} \mathrm{~J}=(0.900 \mathrm{~J} / \mathrm{g} \cdot \mathrm{~K})(295 \mathrm{~g})(\Delta T) \\
& \Delta T=\frac{\left(7.50 \times 10^{4} \mathrm{~J}\right)}{(295 \mathrm{~g})\left(\frac{0.900 \mathrm{~J}}{\mathrm{~g} \cdot \mathrm{~K}}\right)}
\end{aligned}
$$

$$
\Delta T=282.4859 \mathrm{~K}=282.4859^{\circ} \mathrm{C}
$$

(Because the Celsius degree is the same size as the Kelvin degree, $\Delta T$ is the same in either temperature unit.)
$\Delta T=T_{\text {final }}-T_{\text {initial }}$
$T_{\text {final }}=\Delta T+T_{\text {initial }}$
$T_{\text {final }}=282.4859^{\circ} \mathrm{C}+13.00^{\circ} \mathrm{C}=295.49=295^{\circ} \mathrm{C}$
6.25
$q(\mathrm{~J})=c \mathrm{x}$ mass $\mathrm{x} \Delta T$
$-688 \mathrm{~J}=(2.42 \mathrm{~J} / \mathrm{g} \cdot \mathrm{K})(27.7 \mathrm{~g})(\Delta T)$
$(\Delta T)=\frac{(-688 \mathrm{~J})}{(27.7 \mathrm{~g})\left(\frac{2.42 \mathrm{~J}}{\mathrm{~g} \cdot \mathrm{~K}}\right)}=-10.26345 \mathrm{~K}=-10.26345^{\circ} \mathrm{C}$
$\Delta T=T_{\text {final }}-T_{\text {initial }}$
$T_{\text {initial }}=T_{\text {final }}-\Delta T$
$T_{\text {initial }}=32.5^{\circ} \mathrm{C}-\left(-10.26345^{\circ} \mathrm{C}\right)=42.76345=42.8^{\circ} \mathrm{C}$
6.26 Plan: Since the bolts have the same mass and same specific heat capacity, and one must cool as the other heats (the heat lost by the "hot" bolt equals the heat gained by the "cold" bolt), the final temperature is an average of the two initial temperatures.
Solution:
$\left[\frac{\left(T_{1}+T_{2}\right)}{2}\right]=\left[\frac{\left(100 .{ }^{\circ} \mathrm{C}+55^{\circ} \mathrm{C}\right)}{2}\right]=77.5^{\circ} \mathrm{C}$
6.27

$$
\begin{aligned}
& -q_{\text {lost }}=q_{\text {gained }} \\
& -2(\text { mass })\left(c_{\text {Cu }}\right)\left(T_{\text {final }}-105\right)^{\circ} \mathrm{C}=(\text { mass })\left(c_{\mathrm{Cu}}\right)\left(T_{\text {final }}-45\right)^{\circ} \mathrm{C} \\
& -2\left(T_{\text {final }}-105\right)^{\circ} \mathrm{C}=\left(T_{\text {final }}-45\right)^{\circ} \mathrm{C} \\
& 2\left(105^{\circ} \mathrm{C}\right)-2 T_{\text {final }}=T_{\text {final }}-45^{\circ} \mathrm{C} \\
& 210^{\circ} \mathrm{C}+45^{\circ} \mathrm{C}=T_{\text {final }}+2 T_{\text {final }}=3 T_{\text {final }} \\
& \left(255^{\circ} \mathrm{C}\right) / 3=T_{\text {final }}=\mathbf{8 5 . 0}^{\circ} \mathrm{C}
\end{aligned}
$$

6.28 Plan: The heat lost by the water originally at $85^{\circ} \mathrm{C}$ is gained by the water that is originally at $26^{\circ} \mathrm{C}$. Therefore $-q_{\text {lost }}=q_{\text {gained }}$. Both volumes are converted to mass using the density. Solution:
Mass $(\mathrm{g})$ of $75 \mathrm{~mL}=(75 \mathrm{~mL})\left(\frac{1.00 \mathrm{~g}}{1 \mathrm{~mL}}\right)=75 \mathrm{~g} \quad$ Mass $(\mathrm{g})$ of $155 \mathrm{~mL}=(155 \mathrm{~mL})\left(\frac{1.00 \mathrm{~g}}{1 \mathrm{~mL}}\right)=155 \mathrm{~g}$
$-q_{\text {lost }}=q_{\text {gained }}$
$c \mathrm{x}$ mass $\mathrm{x} \Delta T\left(85^{\circ} \mathrm{C}\right.$ water $)=c$ x mass $\mathrm{x} \Delta T\left(26^{\circ} \mathrm{C}\right.$ water $)$
$-\left(4.184 \mathrm{~J} / \mathrm{g}^{\circ} \mathrm{C}\right)(75 \mathrm{~g})\left(T_{\text {final }}-85\right)^{\circ} \mathrm{C}=\left(4.184 \mathrm{~J} / \mathrm{g}^{\circ} \mathrm{C}\right)(155 \mathrm{~g})\left(T_{\text {final }}-26\right)^{\circ} \mathrm{C}$
$-(75 \mathrm{~g})\left(T_{\text {final }}-85\right)^{\circ} \mathrm{C}=(155 \mathrm{~g})\left(T_{\text {final }}-26\right)^{\circ} \mathrm{C}$
$6375-75 T_{\text {final }}=155 T_{\text {final }}-4030$
$6375+4030=155 T_{\text {final }}+75 T_{\text {final }}$
$10405=230 . T_{\text {final }}$
$T_{\text {final }}=(10405 / 230)=45.24=.45^{\circ} \mathrm{C}$
$6.29-q_{\text {lost }}=q_{\text {gained }}$
$-[24.4 \mathrm{~mL}(1.00 \mathrm{~g} / \mathrm{mL})]\left(4.184 \mathrm{~J} / \mathrm{g}^{\circ} \mathrm{C}\right)(23.5-35.0)^{\circ} \mathrm{C}=($ mass $)\left(4.184 \mathrm{~J} / \mathrm{g}^{\circ} \mathrm{C}\right)(23.5-18.2)^{\circ} \mathrm{C}$
$-(24.4)(23.5-35.0)=($ mass $)(23.5-18.2)$
$-(24.4)(-11.5)=($ mass $)(5.3)$
280.6 = (mass)(5.3)
$52.943 \mathrm{~g}=$ mass
Volume $(\mathrm{mL})=(52.943 \mathrm{~g})\left(\frac{1 \mathrm{~mL}}{1.00 \mathrm{~g}}\right)=52.943=53 \mathrm{~mL}$
6.30 Benzoic acid is $\mathrm{C}_{6} \mathrm{H}_{5} \mathrm{COOH}$, and will be symbolized as HBz .
$-q_{\text {reaction }}=q_{\text {water }}+q_{\text {calorimeter }}$
$-q_{\text {reaction }}=-(1.221 \mathrm{~g} \mathrm{HBz})\left(\frac{1 \mathrm{~mol} \mathrm{HBz}}{122.12 \mathrm{~g} \mathrm{HBz}}\right)\left(\frac{-3227 \mathrm{~kJ}}{1 \mathrm{~mol} \mathrm{HBz}}\right)\left(\frac{10^{3} \mathrm{~J}}{1 \mathrm{~kJ}}\right)=3.226472 \times 10^{4} \mathrm{~J}$
$q_{\text {water }}=c \times$ mass $\times \Delta T=4.184 \mathrm{~J} / \mathrm{g}^{\circ} \mathrm{C} \times 1200 \mathrm{~g} \mathrm{x} \Delta T$
$q_{\text {calorimeter }}=C \times \Delta T=1365 \mathrm{~J} /{ }^{\circ} \mathrm{C} \times \Delta T$
$-q_{\text {reaction }}=q_{\text {water }}+q_{\text {calorimeter }}$
$3.226472 \times 10^{4} \mathrm{~J}=4.184 \mathrm{~J} / \mathrm{g}^{\circ} \mathrm{C} \times 1200 \mathrm{~g} \mathrm{x} \Delta T+1365 \mathrm{~J} /{ }^{\circ} \mathrm{C} \times \Delta T$
$3.226472 \times 10^{4} \mathrm{~J}=5020.8(\Delta T)+1365(\Delta T)$
$3.226472 \times 10^{4} \mathrm{~J}=6385.8(\Delta T)$
$\Delta T=3.226472 \times 10^{4} / 6385.8=5.052573=5.053^{\circ} \mathbf{C}$
6.31 a) Energy will flow from Cu (at $100.0^{\circ} \mathrm{C}$ ) to Fe (at $0.0^{\circ} \mathrm{C}$ ).
b) To determine the final temperature, the heat capacity of the calorimeter must be known.
c) $-q_{\mathrm{Cu}}=q_{\mathrm{Fe}}+q_{\text {calorimeter }}$ assume $q_{\text {calorimeter }}=0$.
$-q_{\mathrm{Cu}}=q_{\mathrm{Fe}}+0$
$-(20.0 \mathrm{~g} \mathrm{Cu})\left(0.387 \mathrm{~J} / \mathrm{g}^{\circ} \mathrm{C}\right)\left(T_{\text {final }}-100.0\right)^{\circ} \mathrm{C}=(30.0 \mathrm{~g} \mathrm{Fe})\left(0.450 \mathrm{~J} / \mathrm{g}^{\circ} \mathrm{C}\right)\left(T_{\text {final }}-0.0\right)^{\circ} \mathrm{C}+0.0 \mathrm{~J}$
$-(20.0 \mathrm{~g})\left(0.387 \mathrm{~J} / \mathrm{g}^{\circ} \mathrm{C}\right)\left(T_{\text {final }}-100.0^{\circ} \mathrm{C}\right)=(30.0 \mathrm{~g})\left(0.450 \mathrm{~J} / \mathrm{g}^{\circ} \mathrm{C}\right)\left(T_{\text {final }}-0.0^{\circ} \mathrm{C}\right)$
$-(7.74)\left(T_{\text {final }}-100.0\right)=(13.5)\left(T_{\text {final }}-0.0\right)$
$774-7.74 T_{\text {final }}=13.5 T_{\text {final }}$
$774=(13.5+7.74) T_{\text {final }}=21.24 T_{\text {final }}$
$T_{\text {final }}=774 / 21.24=36.44068=36.4^{\circ} \mathrm{C}$
6.32 The reaction is: $2 \mathrm{KOH}(a q)+\mathrm{H}_{2} \mathrm{SO}_{4}(a q) \rightarrow \mathrm{K}_{2} \mathrm{SO}_{4}(a q)+2 \mathrm{H}_{2} \mathrm{O}(l)$
$q(\mathrm{~kJ})=(25.0+25.0) \mathrm{mL}(1.00 \mathrm{~g} / \mathrm{mL})\left(4.184 \mathrm{~J} / \mathrm{g}^{\circ} \mathrm{C}\right)(30.17-23.50)^{\circ} \mathrm{C}\left(1 \mathrm{~kJ} / 10^{3} \mathrm{~J}\right)=1.395364 \mathrm{~kJ}$
(The temperature increased so the heat of reaction is exothermic.)
Amount (moles) of $\mathrm{H}_{2} \mathrm{SO}_{4}=(25.0 \mathrm{~mL})\left(0.500 \mathrm{~mol} \mathrm{H}_{2} \mathrm{SO}_{4} / \mathrm{L}\right)\left(10^{-3} \mathrm{~L} / 1 \mathrm{~mL}\right)=0.0125 \mathrm{~mol} \mathrm{H}_{2} \mathrm{SO}_{4}$
Amount (moles) of $\mathrm{KOH}=(25.0 \mathrm{~mL})(1.00 \mathrm{~mol} \mathrm{KOH} / \mathrm{L})\left(10^{-3} \mathrm{~L} / 1 \mathrm{~mL}\right)=0.0250 \mathrm{~mol} \mathrm{KOH}$
The moles show that both $\mathrm{H}_{2} \mathrm{SO}_{4}$ and KOH are limiting.
The enthalpy change could be calculated in any of the following ways:
$\Delta H=-1.395364 \mathrm{~kJ} / 0.0125 \mathrm{~mol} \mathrm{H}_{2} \mathrm{SO}_{4}=-111.62912=-112 \mathbf{k J} / \mathbf{m o l ~ H}_{2} \mathbf{S O}_{4}$
$\Delta H=-1.395364 \mathrm{~kJ} / 0.0250 \mathrm{~mol} \mathrm{KOH}=-55.81456=-55.8 \mathrm{~kJ} / \mathbf{m o l ~ K O H}$
(Per mole of $\mathrm{K}_{2} \mathrm{SO}_{4}$ gives the same value as per mole of $\mathrm{H}_{2} \mathrm{SO}_{4}$, and per mole of $\mathrm{H}_{2} \mathrm{O}$ gives the same value as per mole of KOH .)
6.33 Plan: Recall that $\Delta H$ is positive for an endothermic reaction in which heat is absorbed, while $\Delta H$ is negative for an
exothermic reaction in which heat is released.
Solution:
The reaction has a positive $\Delta \boldsymbol{H}_{\mathrm{rxn}}$, because this reaction requires the input of energy to break the oxygen-oxygen bond in $\mathrm{O}_{2}$ :

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\mathrm{O}_{2}(\mathrm{~g})+\text { energy } \rightarrow 2 \mathrm{O}(\mathrm{~g})
$$

6.34 Plan: Recall that $\Delta H$ is positive for an endothermic reaction in which heat is absorbed, while $\Delta H$ is negative for
exothermic reaction in which heat is released.
Solution:
As a substance changes from the gaseous state to the liquid state, energy is released so $\Delta H$ would be negative for the condensation of 1 mol of water. The value of $\Delta H$ for the vaporization of 2 mol of water would be twice the value of $\Delta H$ for the condensation of 1 mol of water vapor but would have an opposite sign $(+\Delta H)$.

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\begin{array}{cr}
\mathrm{H}_{2} \mathrm{O}(\mathrm{~g}) \rightarrow \mathrm{H}_{2} \mathrm{O}(\mathrm{l})+\text { Energy } & 2 \mathrm{H}_{2} \mathrm{O}(\mathrm{l})+\text { Energy } \rightarrow 2 \mathrm{H}_{2} \mathrm{O}(\mathrm{~g}) \\
\Delta H_{\text {condensation }}=(-) & \Delta H_{\text {vaporization }}=(+) 2\left[\Delta H_{\text {condensation }}\right]
\end{array}
$$

The enthalpy for 1 mole of water condensing would be opposite in sign to and one-half the value for the conversion of 2 moles of liquid $\mathrm{H}_{2} \mathrm{O}$ to $\mathrm{H}_{2} \mathrm{O}$ vapor.
6.35 Plan: Recall that $\Delta H$ is positive for an endothermic reaction in which heat is absorbed, while $\Delta H$ is negative for an exothermic reaction in which heat is released. The $\Delta H_{\mathrm{rxn}}$ is specific for the reaction as written, meaning that 20.2 kJ is released when one-eighth of a mole of sulfur reacts. Use the ratio between moles of sulfur and $\Delta H$ to convert between amount of sulfur and heat released.
Solution:
a) This reaction is exothermic because $\Delta H$ is negative.
b) Because $\Delta H$ is a state function, the total energy required for the reverse reaction, regardless of how the change occurs, is the same magnitude but different sign of the forward reaction. Therefore, $\Delta H=+20.2 \mathbf{k J}$.
c) $\Delta H_{\mathrm{rxn}}=\left(2.6 \mathrm{~mol} \mathrm{~S}_{8}\right)\left(\frac{-20.2 \mathrm{~kJ}}{(1 / 8) \mathrm{mol} \mathrm{S}_{8}}\right)=-420.16=-\mathbf{4 . 2 \times 1 0 ^ { 2 } \mathbf { ~ k J }}$
d) The mass of $S_{8}$ requires conversion to moles and then a calculation identical to part c) can be performed.
$\Delta H_{\mathrm{rxn}}=\left(25.0 \mathrm{~g} \mathrm{~S}_{8}\right)\left(\frac{1 \mathrm{~mol} \mathrm{~S}_{8}}{256.56 \mathrm{~g} \mathrm{~S}_{8}}\right)\left(\frac{-20.2 \mathrm{~kJ}}{(1 / 8) \mathrm{mol} \mathrm{S}_{8}}\right)=-15.7468=\mathbf{- 1 5 . 7} \mathbf{~ k J}$
6.36 $\quad \mathrm{MgCO}_{3}(s) \rightarrow \mathrm{MgO}(s)+\mathrm{CO}_{2}(g)$

$$
\Delta H_{\mathrm{rxn}}=117.3 \mathrm{~kJ}
$$

a) Absorbed
b) $\Delta H_{\mathrm{rxn}}$ (reverse) $=\mathbf{- 1 1 7 . 3} \mathbf{~ k J}$
c) $\Delta H_{\mathrm{rxn}}=(5.35 \mathrm{~mol} \mathrm{CO} 2)\left(\frac{-117.3 \mathrm{~kJ}}{1 \mathrm{~mol} \mathrm{CO}_{2}}\right)=-627.555=\mathbf{- 6 2 8} \mathbf{~ k J}$
d) $\Delta H_{\mathrm{rxn}}=\left(35.5 \mathrm{~g} \mathrm{CO}_{2}\right)\left(\frac{1 \mathrm{~mol} \mathrm{CO}_{2}}{44.01 \mathrm{~g} \mathrm{CO}_{2}}\right)\left(\frac{-117.3 \mathrm{~kJ}}{1 \mathrm{~mol} \mathrm{CO}_{2}}\right)=-94.618=-\mathbf{9 4 . 6} \mathbf{~ k J}$
6.37 Plan: A thermochemical equation is a balanced equation that includes the heat of reaction. Since heat is absorbed in this reaction, $\Delta H$ will be positive. Convert the mass of NO to moles and use the ratio between NO and $\Delta H$ to find the heat involved for this amount of NO.
Solution:
a) $1 / 2 \mathrm{~N}_{2}(g)+1 / 2 \mathrm{O}_{2}(g) \rightarrow \mathrm{NO}(g) \quad \Delta H=90.29 \mathrm{~kJ}$
b) $\Delta H_{\mathrm{rxn}}=(3.50 \mathrm{~g} \mathrm{NO})\left(\frac{1 \mathrm{~mol} \mathrm{NO}}{30.01 \mathrm{~g} \mathrm{NO}}\right)\left(\frac{-90.29 \mathrm{~kJ}}{1 \mathrm{~mol} \mathrm{NO}}\right)=-10.5303=\mathbf{- 1 0 . 5} \mathbf{~ k J}$
6.38
a) $\mathrm{KBr}(\mathrm{s}) \rightarrow \mathrm{K}(\mathrm{s})+1 / 2 \mathrm{Br}_{2}(l) \quad \Delta H_{\mathrm{rxn}}=394 \mathrm{~kJ}$
b) $\Delta H_{\mathrm{rxn}}=(10.0 \mathrm{~kg} \mathrm{KBr})\left(\frac{10^{3} \mathrm{~g}}{1 \mathrm{~kg}}\right)\left(\frac{1 \mathrm{~mol} \mathrm{KBr}}{119.00 \mathrm{~g} \mathrm{KBr}}\right)\left(\frac{-394 \mathrm{~kJ}}{1 \mathrm{~mol} \mathrm{KBr}}\right)=-3.3109 \times 10^{4}=-\mathbf{3 . 3 1 \times 1 0} \mathbf{x}^{4} \mathbf{~ k J}$
6.39 Plan: For the reaction written, 2 moles of $\mathrm{H}_{2} \mathrm{O}_{2}$ release 196.1 kJ of energy upon decomposition. Use this ratio to convert between the given amount of reactant and the amount of heat released. The amount of $\mathrm{H}_{2} \mathrm{O}_{2}$ must be converted from kg to g to moles.
Solution:

$$
2 \mathrm{H}_{2} \mathrm{O}_{2}(l) \rightarrow 2 \mathrm{H}_{2} \mathrm{O}(l)+\mathrm{O}_{2}(g) \quad \Delta H_{\mathrm{rxn}}=-196.1 \mathrm{~kJ}
$$

Heat $(\mathrm{kJ})=q=\left(652 \mathrm{~kg} \mathrm{H}_{2} \mathrm{O}_{2}\right)\left(\frac{10^{3} \mathrm{~g}}{1 \mathrm{~kg}}\right)\left(\frac{1 \mathrm{~mol} \mathrm{H}_{2} \mathrm{O}_{2}}{34.02 \mathrm{~g} \mathrm{H}_{2} \mathrm{O}_{2}}\right)\left(\frac{-196.1 \mathrm{~kJ}}{2 \mathrm{~mol} \mathrm{H}_{2} \mathrm{O}_{2}}\right)=-1.87915 \times 10^{6}=\mathbf{- 1 . 8 8 \times 1 0} \mathbf{0}^{\mathbf{6}} \mathbf{k J}$
6.40 For the reaction written, 1 mole of $\mathrm{B}_{2} \mathrm{H}_{6}$ releases 755.4 kJ of energy upon reaction.
$\mathrm{B}_{2} \mathrm{H}_{6}(\mathrm{~g})+6 \mathrm{Cl}_{2}(g) \rightarrow 2 \mathrm{BCl}_{3}(\mathrm{~g})+6 \mathrm{HCl}(\mathrm{g}) \quad \Delta H_{\mathrm{rxn}}=-755.4 \mathrm{~kJ}$
Heat $(\mathrm{kJ})=q=(1 \mathrm{~kg})\left(\frac{10^{3} \mathrm{~g}}{1 \mathrm{~kg}}\right)\left(\frac{1 \mathrm{~mol}_{2} \mathrm{H}_{6}}{27.67 \mathrm{~g} \mathrm{~B}_{2} \mathrm{H}_{6}}\right)\left(\frac{-755.4 \mathrm{~kJ}}{1 \mathrm{~mol} \mathrm{~B}_{2} \mathrm{H}_{6}}\right)=-2.73003 \times 10^{4}=-\mathbf{2 . 7 3 0 \times 1 0} \mathbf{~ k J} / \mathbf{k g}$
6.41 Plan: A thermochemical equation is a balanced equation that includes the heat of reaction. Heat is released in this reaction so $\Delta H$ is negative. Use the ratio between $\Delta H$ and moles of $\mathrm{C}_{2} \mathrm{H}_{4}$ to find the amount of $\mathrm{C}_{2} \mathrm{H}_{4}$ that must react to produce the given quantity of heat.
Solution:
a) $\mathrm{C}_{2} \mathrm{H}_{4}(g)+3 \mathrm{O}_{2}(g) \rightarrow 2 \mathrm{CO}_{2}(g)+2 \mathrm{H}_{2} \mathrm{O}(g) \quad \Delta H_{\mathrm{rxn}}=-1411 \mathrm{~kJ}$
b) Mass (g) of $\mathrm{C}_{2} \mathrm{H}_{4}=(-70.0 \mathrm{~kJ})\left(\frac{1 \mathrm{~mol} \mathrm{C}_{2} \mathrm{H}_{4}}{-1411 \mathrm{~kJ}}\right)\left(\frac{28.05 \mathrm{~g} \mathrm{C}_{2} \mathrm{H}_{4}}{1 \mathrm{~mol} \mathrm{C}_{2} \mathrm{H}_{4}}\right)=1.39157=\mathbf{1 . 3 9} \mathbf{g ~ C}_{2} \mathbf{H}_{4}$
a) $\mathrm{C}_{12} \mathrm{H}_{22} \mathrm{O}_{11}(\mathrm{~s})+12 \mathrm{O}_{2}(\mathrm{~g}) \rightarrow 12 \mathrm{CO}_{2}(\mathrm{~g})+11 \mathrm{H}_{2} \mathrm{O}(\mathrm{g}) \Delta H_{\mathrm{rxn}}=-5.64 \times 10^{3} \mathrm{~kJ}$ b) Heat $(\mathrm{kJ})=q=\left(1 \mathrm{~g} \mathrm{C}_{12} \mathrm{H}_{22} \mathrm{O}_{11}\right)\left(\frac{1 \mathrm{~mol} \mathrm{C}_{12} \mathrm{H}_{22} \mathrm{O}_{11}}{342.30 \mathrm{~g} \mathrm{C}_{12} \mathrm{H}_{22} \mathrm{O}_{11}}\right)\left(\frac{-5.64 \times 10^{3} \mathrm{~kJ}}{1 \mathrm{~mol} \mathrm{C}_{12} \mathrm{H}_{22} \mathrm{O}_{11}}\right)=-16.47677=\mathbf{- 1 6 . 5} \mathbf{~ k J} / \mathbf{g}$
6.43 Hess's law: $\Delta H_{\mathrm{rxn}}$ is independent of the number of steps or the path of the reaction.
6.44 Plan: To obtain the overall reaction, add the first reaction to the reverse of the second. When the second reaction is reversed, the sign of its enthalpy change is reversed from positive to negative.
Solution:

| $\mathrm{Ca}(\mathrm{s})+1 / 2 \mathrm{O}_{2}(g) \rightarrow \mathrm{CaO}(s)$ | $\Delta H=-635.1 \mathrm{~kJ}$ |
| :--- | :--- |
| $\mathrm{GaO}(s)+\mathrm{CO}_{2}(g) \rightarrow \mathrm{CaCO}_{3}(s)$ | $\Delta H=-178.3 \mathrm{~kJ}$ (reaction is reversed) |
| $\mathrm{Ca}(s)+1 / 2 \mathrm{O}_{2}(g)+\mathrm{CO}_{2}(g) \rightarrow \mathrm{CaCO}_{3}(\mathrm{~s})$ | $\Delta H=-\mathbf{8 1 3 . 4} \mathrm{kJ}$ |
| $(g) \rightarrow 2 \mathrm{NO}(g)+\mathrm{Cl}_{2}(g)$ | $\Delta H=-2(-38.6 \mathrm{~kJ})$ |
| $\rightarrow \mathrm{N}_{2}(g)+\mathrm{O}_{2}(g)$ | $\Delta H=-2(90.3 \mathrm{~kJ})$ |
| $(g) \rightarrow \mathrm{N}_{2}(g)+\mathrm{O}_{2}(g)+\mathrm{Cl}_{2}(g)$ | $\Delta H=77.2 \mathrm{~kJ}+(-180.6 \mathrm{~kJ})=\mathbf{- 1 0 3 . 4} \mathbf{~ k J}$ |

6.46 Plan: Add the two equations, canceling substances that appear on both sides of the arrow. When matching the equations with the arrows in the Figure, remember that a positive $\Delta H$ corresponds to an arrow pointing up while a negative $\Delta H$ corresponds to an arrow pointing down.

Solution:

| 1) | $\mathrm{N}_{2}(\mathrm{~g})+\mathrm{O}_{2}(\mathrm{~g}) \rightarrow$ 2 $\mathrm{NO}(g)$ | $\Delta H=180.6 \mathrm{~kJ}$ |
| :---: | :---: | :---: |
| 2) | $2 \mathrm{NO}(\mathrm{g})+\mathrm{O}_{2}(\mathrm{~g}) \rightarrow 2 \mathrm{NO}_{2}(\mathrm{~g})$ | $\Delta H=-114.2 \mathrm{~kJ}$ |
| 3) | $\mathrm{N}_{2}(\mathrm{~g})+2 \mathrm{O}_{2}(\mathrm{~g}) \rightarrow \mathbf{2} \mathrm{NO}_{2}(\mathrm{~g})$ | $\Delta H_{\mathrm{rxn}}=+66.4 \mathrm{~kJ}$ |

In Figure P6.46, A represents reaction 1 with a larger amount of energy absorbed, $\mathbf{B}$ represents reaction 2 with a smaller amount of energy released, and $\mathbf{C}$ represents reaction 3 as the sum of $A$ and $B$.

| 1) | $\mathrm{P}_{4}(\mathrm{~s})+6 \mathrm{Cl}_{2}(\mathrm{~g}) \rightarrow 4 \mathrm{PCl}_{3}(\mathrm{~g})$ | $\Delta H_{1}=-1148 \mathrm{~kJ}$ |  |
| :--- | :--- | :--- | :--- |
| 2) | $4 \mathrm{PCl}_{3}(g)+4 \mathrm{Cl}_{2}(g) \rightarrow 4 \mathrm{PCl}_{5}(\mathrm{~g})$ | $\Delta H_{2}=-460 \mathrm{~kJ}$ |  |
| 3) | $\mathbf{P}_{\mathbf{4}}(\mathbf{s})+\mathbf{1 0 C l} \mathbf{2}(\boldsymbol{g}) \rightarrow \mathbf{4} \mathbf{P C l}_{\mathbf{5}}(\mathrm{g})$ | $\Delta \boldsymbol{H}_{\text {overall }}$ | $=\mathbf{- 1 6 0 8} \mathbf{~ k J}$ | Equation 1) $=B$, equation 2) $=C$, equation 3) $=A$

C (diamond) $+\mathrm{\theta}_{z}(\mathrm{~g}) \rightarrow \mathrm{EO}_{z}(\mathrm{~g})$
$\Delta H=-395.4 \mathrm{~kJ}$
$\mathrm{CO}_{z}(\mathrm{~g}) \rightarrow \mathrm{C}$ (graphite) $+\mathrm{O}_{z}(\mathrm{~g})$ $\Delta H=-(-393.5 \mathrm{~kJ})$
$\overline{\mathrm{C}}$ (diamond) $\rightarrow$ C(graphite)
$\Delta H=-1.9 \mathbf{k J}$
6.49 The standard heat of reaction, $\Delta H_{\mathrm{rxn}}^{\circ}$, is the enthalpy change for any reaction where all substances are in their standard states. The standard heat of formation, $\Delta H_{\mathrm{f}}^{\circ}$, is the enthalpy change that accompanies the formation of one mole of a compound in its standard state from elements in their standard states. Standard state is 1 atm for gases, 1 M for solutes, and the most stable form for liquids and solids. Standard state does not include a specific temperature, but a temperature must be specified in a table of standard values.
6.50 Plan: $\Delta H_{\mathrm{f}}^{\circ}$ is for the reaction that shows the formation of one mole of compound from its elements in their standard states.
Solution:
a) $1 / 2 \mathrm{Cl}_{2}(g)+\mathrm{Na}(s) \rightarrow \mathrm{NaCl}(s)$ The element chlorine occurs as $\mathrm{Cl}_{2}$, not Cl .
b) $\mathrm{H}_{2}(\mathrm{~g})+1 / 2 \mathrm{O}_{2}(\mathrm{~g}) \rightarrow \mathrm{H}_{2} \mathrm{O}(\mathrm{g})$ The element hydrogen exists as $\mathrm{H}_{2}$, not H , and the formation of water is written with water as the product.
c) No changes
6.51 Plan: Formation equations show the formation of one mole of compound from its elements. The elements must be in their most stable states ( $\Delta H_{\mathrm{f}}^{\circ}=0$ ).
Solution:
a) $\mathrm{Ca}(\mathrm{s})+\mathrm{Cl}_{2}(\mathrm{~g}) \rightarrow \mathrm{CaCl}_{2}(\mathrm{~s})$
b) $\mathrm{Na}(\mathrm{s})+1 / 2 \mathrm{H}_{2}(g)+\mathrm{C}$ (graphite) $+3 / 2 \mathrm{O}_{2}(g) \rightarrow \mathrm{NaHCO}_{3}(s)$
c) C (graphite) $+2 \mathrm{Cl}_{2}(g) \rightarrow \mathrm{CCl}_{4}(\mathrm{l})$
d) $1 / 2 \mathrm{H}_{2}(g)+1 / 2 \mathrm{~N}_{2}(g)+3 / 2 \mathrm{O}_{2}(g) \rightarrow \mathrm{HNO}_{3}(l)$
a) $1 / 2 \mathrm{H}_{2}(g)+1 / 2 \mathrm{I}_{2}(\mathrm{~s}) \rightarrow \mathrm{HI}(g)$
b) $\mathrm{Si}(\mathrm{s})+2 \mathrm{~F}_{2}(\mathrm{~g}) \rightarrow \mathrm{SiF}_{4}(\mathrm{~g})$
c) $3 / 2 \mathrm{O}_{2}(\mathrm{~g}) \rightarrow \mathrm{O}_{3}(\mathrm{~g})$
d) $3 \mathrm{Ca}(\mathrm{s})+1 / 2 \mathrm{P}_{4}(\mathrm{~s})+4 \mathrm{O}_{2}(\mathrm{~g}) \rightarrow \mathrm{Ca}_{3}\left(\mathrm{PO}_{4}\right)_{2}(\mathrm{~s})$

Plan: The enthalpy change of a reaction is the sum of the heats of formation of the products minus the sum of the heats of formation of the reactants. Since the $\Delta H_{\mathrm{f}}^{\circ}$ values (Appendix B) are reported as energy per one mole, use the appropriate stoichiometric coefficient to reflect the higher number of moles.

Solution:
$\Delta H_{\mathrm{rxn}}^{\circ}=\sum m \Delta H_{\mathrm{f}}^{\circ}$ (products) $-\sum \mathrm{n} \Delta H_{\mathrm{f}}^{\circ}$ (reactants)

$$
\text { a) } \begin{aligned}
\Delta H_{\mathrm{rxn}}^{\circ} & =\left\{2 \Delta H_{\mathrm{f}}^{\circ}\left[\mathrm{SO}_{2}(\mathrm{~g})\right]+2 \Delta H_{\mathrm{f}}^{\circ}\left[\mathrm{H}_{2} \mathrm{O}(\mathrm{~g})\right]\right\}-\left\{2 \Delta H_{\mathrm{f}}^{\circ}\left[\mathrm{H}_{2} \mathrm{~S}(\mathrm{~g})\right]+3 \Delta H_{\mathrm{f}}^{\circ}\left[\mathrm{O}_{2}(\mathrm{~g})\right]\right\} \\
& =[(2 \mathrm{~mol})(-296.8 \mathrm{~kJ} / \mathrm{mol})+(2 \mathrm{~mol})(-241.826 \mathrm{~kJ} / \mathrm{mol})]-[(2 \mathrm{~mol})(-20.2 \mathrm{~kJ} / \mathrm{mol})+(3 \mathrm{~mol})(0.0 \mathrm{~kJ} / \mathrm{mol})] \\
& =-\mathbf{1 0 3 6 . 9} \mathbf{~ k J}
\end{aligned}
$$

b) The balanced equation is $\mathrm{CH}_{4}(g)+4 \mathrm{Cl}_{2}(g) \rightarrow \mathrm{CCl}_{4}(l)+4 \mathrm{HCl}(g)$

$$
\begin{aligned}
\Delta H_{\mathrm{rxn}}^{\circ} & =\left\{1 \Delta H_{\mathrm{f}}^{\circ}\left[\mathrm{CCl}_{4}(\mathrm{l})\right]+4 \Delta H_{\mathrm{f}}^{\circ}[\mathrm{HCl}(\mathrm{~g})]\right\}-\left\{1 \Delta H_{\mathrm{f}}^{\circ}\left[\mathrm{CH}_{4}(\mathrm{~g})\right]+4 \Delta H_{\mathrm{f}}^{\circ}\left[\mathrm{Cl}_{2}(g)\right]\right\} \\
\Delta H_{\mathrm{rxn}}^{\circ} & =[(1 \mathrm{~mol})(-139 \mathrm{~kJ} / \mathrm{mol})+(4 \mathrm{~mol})(-92.31 \mathrm{~kJ} / \mathrm{mol})]-[(1 \mathrm{~mol})(-74.87 \mathrm{~kJ} / \mathrm{mol})+(4 \mathrm{~mol})(0 \mathrm{~kJ} / \mathrm{mol})] \\
& =-433 \mathrm{~kJ}
\end{aligned}
$$

$$
\Delta H_{\mathrm{rxn}}^{\circ}=\sum m \Delta H_{\mathrm{f} \text { (products) }}^{\circ}-\sum n \Delta H_{\mathrm{f} \text { (reactants) }}^{\circ}
$$

a) $\Delta H_{\mathrm{rxn}}^{\circ}=\left\{1 \Delta H_{\mathrm{f}}^{\circ}\left[\mathrm{SiF}_{4}(\mathrm{~g})\right]+2 \Delta H_{\mathrm{f}}^{\circ}\left[\mathrm{H}_{2} \mathrm{O}(\mathrm{l})\right]\right\}-\left\{1 \Delta H_{\mathrm{f}}^{\circ}\left[\mathrm{SiO}_{2}(\mathrm{~s})\right]+4 \Delta H_{\mathrm{f}}^{\circ}[\mathrm{HF}(\mathrm{g})]\right\}$

$$
=[(1 \mathrm{~mol})(-1614.9 \mathrm{~kJ} / \mathrm{mol})+(2 \mathrm{~mol})(-285.840 \mathrm{~kJ} / \mathrm{mol})]
$$

$$
=-184 \mathrm{~kJ}
$$

$$
-[(1 \mathrm{~mol})(-910.9 \mathrm{~kJ} / \mathrm{mol})+(4 \mathrm{~mol})(-273 \mathrm{~kJ} / \mathrm{mol})]
$$

b) $2 \mathrm{C}_{2} \mathrm{H}_{6}(\mathrm{~g})+7 \mathrm{O}_{2}(\mathrm{~g}) \rightarrow 4 \mathrm{CO}_{2}(\mathrm{~g})+6 \mathrm{H}_{2} \mathrm{O}(\mathrm{g})$

$$
\begin{aligned}
\Delta H_{\mathrm{rxn}}^{\circ} & =\left\{4 \Delta H_{\mathrm{f}}^{\circ}\left[\mathrm{CO}_{2}(\mathrm{~g})\right]+6 \Delta H_{\mathrm{f}}^{\circ}\left[\mathrm{H}_{2} \mathrm{O}(\mathrm{~g})\right]\right\}-\left\{2 \Delta H_{\mathrm{f}}^{\circ}\left[\mathrm{C}_{2} \mathrm{H}_{6}(\mathrm{~g})\right]+7 \Delta H_{\mathrm{f}}^{\circ}\left[\mathrm{O}_{2}(\mathrm{~g})\right]\right\} \\
& =[(4 \mathrm{~mol})(-393.5 \mathrm{~kJ} / \mathrm{mol})+(6 \mathrm{~mol})(-241.826 \mathrm{~kJ} / \mathrm{mol})]-[(2 \mathrm{~mol})(-84.667 \mathrm{~kJ} / \mathrm{mol})+(7 \mathrm{~mol})(0 \mathrm{~kJ} / \mathrm{mol})] \\
& =-\mathbf{2 8 5 5 . 6} \mathbf{~ k J}\left(\text { or }-1427.8 \mathrm{~kJ} \text { for reaction of } 1 \mathrm{~mol} \text { of } \mathrm{C}_{2} \mathrm{H}_{6}\right)
\end{aligned}
$$

Plan: The enthalpy change of a reaction is the sum of the heats of formation of the products minus the sum of the heats of formation of the reactants. Since the $\Delta H_{\mathrm{f}}^{\circ}$ values (Appendix B) are reported as energy per one mole, use the appropriate stoichiometric coefficient to reflect the higher number of moles. In this case, $\Delta H_{\mathrm{rxn}}^{\circ}$ is known and $\Delta H_{\mathrm{f}}^{\circ}$ of CuO must be calculated.

## Solution:

$$
\begin{aligned}
& \Delta H_{\mathrm{rxn}}^{\circ}=\sum m \Delta H_{\mathrm{f}}^{\circ}(\text { products })-\sum n \Delta H_{\mathrm{f}}^{\circ} \text { (reactants) } \\
& \mathrm{Cu}_{2} \mathrm{O}(\mathrm{~s})+1 / 2 \mathrm{O}_{2}(g) \rightarrow 2 \mathrm{CuO}(\mathrm{~s}) \quad \Delta H_{\mathrm{rxn}}^{\circ}=-146.0 \mathrm{~kJ} \\
& \Delta H_{\mathrm{rxn}}^{\circ}=\left\{2 \Delta H_{\mathrm{f}}^{\circ}[\mathrm{CuO}(\mathrm{~s})]\right\}-\left\{1 \Delta H_{\mathrm{f}}^{\circ}\left[\mathrm{Cu}_{2} \mathrm{O}(\mathrm{~s})\right]+1 / 2 \Delta H_{\mathrm{f}}^{\circ}\left[\mathrm{O}_{2}(\mathrm{~g})\right]\right\} \\
& -146.0 \mathrm{~kJ}=\left\{(2 \mathrm{~mol}) \Delta H_{\mathrm{f}}^{\circ}[\mathrm{CuO}(\mathrm{~s})]\right\}-\{(1 \mathrm{~mol})(-168.6 \mathrm{~kJ} / \mathrm{mol})+(1 / 2 \mathrm{~mol})(0 \mathrm{~kJ} / \mathrm{mol})\} \\
& -146.0 \mathrm{~kJ}=2 \mathrm{~mol} \Delta H_{\mathrm{f}}^{\circ}[\mathrm{CuO}(\mathrm{~s})]+168.6 \mathrm{~kJ} \\
& \Delta H_{\mathrm{f}}^{\circ}[\mathrm{CuO}(\mathrm{~s})]=-\frac{314.6 \mathrm{~kJ}}{2 \mathrm{~mol}}=-\mathbf{1 5 7 . 3} \mathrm{kJ} / \mathrm{mol} \\
& \Delta H_{\mathrm{rxn}}^{\circ}=\sum m \Delta H_{\mathrm{f}}^{\circ}(\text { products })-\sum n \Delta H_{\mathrm{f}}^{\circ}(\text { reactants }) \\
& \mathrm{C}_{2} \mathrm{H}_{2}(g)+5 / 2 \mathrm{O}_{2}(g) \rightarrow 2 \mathrm{CO}_{2}(g)+\mathrm{H}_{2} \mathrm{O}(\mathrm{~g}) \quad \Delta H_{\mathrm{rxn}}^{\circ}=-1255.8 \mathrm{~kJ} \\
& \Delta H_{\mathrm{rxn}}^{\circ}=\left\{2 \Delta H_{\mathrm{f}}^{\circ}\left[\mathrm{CO}_{2}(\mathrm{~g})\right]+1 \Delta H_{\mathrm{f}}^{\circ}\left[\mathrm{H}_{2} \mathrm{O}(\mathrm{~g})\right]\right\}-\left\{1 \Delta H_{\mathrm{f}}^{\circ}\left[\mathrm{C}_{2} \mathrm{H}_{2}(g)\right]+5 / 2 \Delta H_{\mathrm{f}}^{\circ}\left[\mathrm{O}_{2}(\mathrm{~g})\right]\right\} \\
& -1255.8 \mathrm{~kJ}=\left\{(2 \mathrm{~mol})(-393.5 \mathrm{~kJ} / \mathrm{mol})+(1 \mathrm{~mol})\left(-241.826 \mathrm{~kJ} / \mathrm{mol}^{\circ}\right)\right\} \\
& -1255.8 \mathrm{~kJ}=-787.0 \mathrm{~kJ}-241.8 \mathrm{~kJ}-(1 \mathrm{~mol}) \Delta H_{\mathrm{f}}^{\circ}\left[\mathrm{C}_{2} \mathrm{H}_{2}(\mathrm{~g})\right] \\
& \Delta H_{\mathrm{f}}^{\circ}\left[\mathrm{C}_{2} \mathrm{H}_{2}(g)\right]=\frac{-227.0 \mathrm{~kJ}}{-1 \mathrm{~mol}}=227.0 \mathrm{~kJ} / \mathrm{mol}
\end{aligned}
$$

a) $4 \mathrm{C}_{3} \mathrm{H}_{5}\left(\mathrm{NO}_{3}\right)_{3}(\mathrm{l}) \rightarrow 6 \mathrm{~N}_{2}(\mathrm{~g})+10 \mathrm{H}_{2} \mathrm{O}(\mathrm{g})+12 \mathrm{CO}_{2}(\mathrm{~g})+\mathrm{O}_{2}(\mathrm{~g})$
b) $\Delta H_{\mathrm{rxn}}^{\circ}=\left\{6 \Delta H_{\mathrm{f}}^{\circ}\left[\mathrm{N}_{2}(\mathrm{~g})\right]+10 \Delta H_{\mathrm{f}}^{\circ}\left[\mathrm{H}_{2} \mathrm{O}(\mathrm{g})\right]+12 \Delta H_{\mathrm{f}}^{\circ}\left[\mathrm{CO}_{2}(\mathrm{~g})\right]+1 \Delta H_{\mathrm{f}}^{\circ}\left[\mathrm{O}_{2}(\mathrm{~g})\right]\right\}-\left\{4 \Delta H_{\mathrm{f}}^{\circ}\left[\mathrm{C}_{3} \mathrm{H}_{5}\left(\mathrm{NO}_{3}\right)_{3}(\mathrm{l})\right]\right\}$ $-2.29 \times 10^{4} \mathrm{~kJ}=\{(6 \mathrm{~mol})(0 \mathrm{~kJ} / \mathrm{mol})+(10 \mathrm{~mol})(-241.826 \mathrm{kJmol})+(12 \mathrm{~mol})(-393.5 \mathrm{~kJ} / \mathrm{mol})+(1 \mathrm{~mol})(0 \mathrm{kJmol})\}$

$$
-\left\{(4 \mathrm{~mol}) \Delta H_{\mathrm{f}}^{\circ}\left[\mathrm{C}_{3} \mathrm{H}_{5}\left(\mathrm{NO}_{3}\right)_{3}(\mathrm{l})\right]\right\}
$$

$-2.29 \times 10^{4} \mathrm{~kJ}=-2418 \mathrm{~kJ}-4722 \mathrm{~kJ}-(4 \mathrm{~mol}) \Delta H_{\mathrm{f}}^{\circ}\left[\mathrm{C}_{3} \mathrm{H}_{5}\left(\mathrm{NO}_{3}\right)_{3}(\mathrm{l})\right]$
$\Delta H_{\mathrm{f}}^{\circ}\left[\mathrm{C}_{3} \mathrm{H}_{5}\left(\mathrm{NO}_{3}\right)_{3}(\mathrm{l})\right]=\frac{-15760 \mathrm{~kJ}}{-4 \mathrm{~mol}}=3940 \mathrm{~kJ} / \mathbf{m o l}$

Plan: The enthalpy change of a reaction is the sum of the heats of formation of the products minus the sum of the heats of formation of the reactants. Since the $\Delta H_{f}^{\circ}$ values (Appendix B) are reported as energy per one mole, use the appropriate stoichiometric coefficient to reflect the higher number of moles. Hess's law can also be used to calculate the enthalpy of reaction. In part b), rearrange equations 1) and 2) to give the equation wanted.
Reverse the first equation (changing the sign of $\Delta H_{\mathrm{rxn}}^{\circ}$ ) and multiply the coefficients (and $\Delta H_{\mathrm{rxn}}^{\circ}$ ) of the second reaction by 2 .
Solution:
$2 \mathrm{PbSO}_{4}(s)+2 \mathrm{H}_{2} \mathrm{O}(l) \rightarrow \mathrm{Pb}(s)+\mathrm{PbO}_{2}(s)+2 \mathrm{H}_{2} \mathrm{SO}_{4}(l)$
$\Delta H_{\mathrm{rxn}}^{\circ}=\sum m \Delta H_{\mathrm{f}}^{\circ}$ (products) $-\sum \mathrm{n} \Delta H_{\mathrm{f}}^{\circ}$ (reactants)
a) $\Delta H_{\mathrm{rxn}}^{\circ}=\left\{1 \Delta H_{\mathrm{f}}^{\circ}[\mathrm{Pb}(\mathrm{s})]+1 \Delta H_{\mathrm{f}}^{\circ}\left[\mathrm{PbO}_{2}(\mathrm{~s})\right]+2 \Delta H_{\mathrm{f}}^{\circ}\left[\mathrm{H}_{2} \mathrm{SO}_{4}(\mathrm{l})\right]\right\}$
$-\left\{2 \Delta H_{\mathrm{f}}^{\circ}\left[\mathrm{PbSO}_{4}(\mathrm{~s})\right]+2 \Delta H_{\mathrm{f}}^{\circ}\left[\mathrm{H}_{2} \mathrm{O}(\mathrm{l})\right]\right\}$
$=[(1 \mathrm{~mol})(0 \mathrm{~kJ} / \mathrm{mol})+(1 \mathrm{~mol})(-276.6 \mathrm{kJmol})+(2 \mathrm{~mol})(-813.989 \mathrm{~kJ} / \mathrm{mol})]$
$-[(2 \mathrm{~mol})(-918.39 \mathrm{~kJ} / \mathrm{mol})+(2 \mathrm{~mol})(-285.840 \mathrm{~kJ} / \mathrm{mol})]$
$=503.9 \mathrm{~kJ}$
b) Use Hess's law:

$$
\begin{array}{ll}
\mathrm{PbSO}_{4}(s) \rightarrow \mathrm{Pb}(\mathrm{~s})+\mathrm{PbO}_{2}(\mathrm{~s})+2 \mathrm{SO}_{3}(g) & \Delta H_{\mathrm{rxn}}^{\circ}=-(-768 \mathrm{~kJ}) \text { Equation has been reversed. } \\
2 \mathrm{SO}_{3}(\mathrm{~g})+2 \mathrm{H}_{2} \mathrm{O}(\mathrm{l}) \rightarrow 2 \mathrm{H}_{2} \mathrm{SO}_{4}(\mathrm{l}) & \Delta H_{\mathrm{rxn}}^{\circ}=2(-132 \mathrm{~kJ}) \\
\hline 2 \mathrm{PbSO}_{4}(\mathrm{~s})+2 \mathrm{H}_{2} \mathrm{O}(\mathrm{l}) \rightarrow \mathrm{Pb}(\mathrm{~s})+\mathrm{PbO}_{2}(\mathrm{~s})+2 \mathrm{H}_{2} \mathrm{SO}_{4}(\mathrm{l}) & \Delta H_{\mathrm{rxn}}^{\circ}=\mathbf{5 0 4} \mathbf{~ k J}
\end{array}
$$

Plan: The enthalpy change of a reaction is the sum of the heats of formation of the products minus the sum of the heats of formation of the reactants. Since the $\Delta H_{\mathrm{f}}^{\circ}$ values (Appendix B) are reported as energy per one mole, use the appropriate stoichiometric coefficient to reflect the higher number of moles. Convert the mass of stearic acid to moles and use the ratio between stearic acid and $\Delta H_{\mathrm{rxn}}^{\circ}$ to find the heat involved for this amount of acid. For part d), use the $\mathrm{kcal} / \mathrm{g}$ of fat relationship calculated in part c ) to convert 11.0 g of fat to total kcal and compare to the 100. Cal amount.
Solution:
a) $\mathrm{C}_{18} \mathrm{H}_{36} \mathrm{O}_{2}(\mathrm{~s})+26 \mathrm{O}_{2}(\mathrm{~g}) \rightarrow 18 \mathrm{CO}_{2}(\mathrm{~g})+18 \mathrm{H}_{2} \mathrm{O}(\mathrm{g})$
b) $\Delta H_{\mathrm{rxn}}^{\circ}=\sum m \Delta H_{\mathrm{f}}^{\circ}$ (products) $-\sum n \Delta H_{\mathrm{f}}^{\circ}$ (reactants)

$$
\begin{aligned}
\Delta H_{\mathrm{rxn}}^{\circ} & =\left\{18 \Delta H_{\mathrm{f}}^{\circ}\left[\mathrm{CO}_{2}(\mathrm{~g})\right]+18 \Delta H_{\mathrm{f}}^{\circ}\left[\mathrm{H}_{2} \mathrm{O}(\mathrm{~g})\right]\right\}-\left\{1 \Delta H_{\mathrm{f}}^{\circ}\left[\mathrm{C}_{18} \mathrm{H}_{36} \mathrm{O}_{2}(\mathrm{~s})\right]+26 \Delta H_{\mathrm{f}}^{\circ}\left[\mathrm{O}_{2}(\mathrm{~g})\right]\right\} \\
& =[(18 \mathrm{~mol})(-393.5 \mathrm{~kJ} / \mathrm{mol})+(18 \mathrm{~mol})(-241.826 \mathrm{~kJ} / \mathrm{mol})]-[(1 \mathrm{~mol})(-948 \mathrm{~kJ} / \mathrm{mol})+(26 \mathrm{~mol})(0 \mathrm{~kJ} / \mathrm{mol})] \\
& =-10,487.868=-\mathbf{1 0}, 488 \mathbf{~ k J}
\end{aligned}
$$

c) $q(\mathrm{~kJ})=\left(1.00 \mathrm{~g} \mathrm{C}_{18} \mathrm{H}_{36} \mathrm{O}_{2}\right)\left(\frac{1 \mathrm{~mol} \mathrm{C}_{18} \mathrm{H}_{36} \mathrm{O}_{2}}{284.47 \mathrm{C}_{18} \mathrm{H}_{36} \mathrm{O}_{2}}\right)\left(\frac{-10,487.868 \mathrm{~kJ}}{1 \mathrm{~mol} \mathrm{C}_{18} \mathrm{H}_{36} \mathrm{O}_{2}}\right)=-36.8681=-\mathbf{3 6 . 9} \mathbf{~ k J}$
$q(\mathrm{kcal})=(-36.8681 \mathrm{~kJ})\left(\frac{1 \mathrm{kcal}}{4.184 \mathrm{~kJ}}\right)=-8.811688=\mathbf{- 8 . 8 1} \mathbf{~ k c a l}$
d) $q(\mathrm{kcal})=(11.0 \mathrm{~g}$ fat $)\left[\frac{-8.811688 \mathrm{kcal}}{1.0 \mathrm{~g} \text { fat }}\right]=96.9286=\mathbf{9 6 . 9} \mathbf{~ k c a l}$

Since $1 \mathrm{kcal}=1 \mathrm{Cal}, 96.9 \mathrm{kcal}=96.9 \mathrm{Cal}$. The calculated calorie content is consistent with the package information.
6.60 Plan: Use the ideal gas law, $P V=n R T$, to calculate the volume of one mole of helium at each temperature. Then use the given equation for $\Delta E$ to find the change in internal energy. The equation for work, $w=-P \Delta V$, is needed for part c), and $q_{P}=\Delta E+P \Delta V$ is used for part d). For part e), recall that $\Delta H=q_{P}$.
Solution:
a) $P V=n R T$ or $V=\frac{n R T}{P}$
$T=273+15=288 \mathrm{~K} \quad$ and $\quad T=273+30=303 \mathrm{~K}$
Initial volume $(\mathrm{L})=V=\frac{n R T}{P}=\frac{\left(0.0821 \frac{\mathrm{~L} \cdot \mathrm{~atm}}{\mathrm{~mol} \cdot \mathrm{~K}}\right)(288 \mathrm{~K})}{(1.00 \mathrm{~atm})}=23.6448=\mathbf{2 3 . 6} \mathbf{~ L} / \mathbf{m o l}$
Final volume $(\mathrm{L})=V=\frac{n R T}{P}=\frac{\left(0.0821 \frac{\mathrm{~L} \cdot \mathrm{~atm}}{\mathrm{~mol} \cdot \mathrm{~K}}\right)(303 \mathrm{~K})}{(1.00 \mathrm{~atm})}=24.8763=\mathbf{2 4 . 9} \mathbf{~ L} / \mathbf{m o l}$
b) Internal energy is the sum of the potential and kinetic energies of each He atom in the system (the balloon). The energy of one mole of helium atoms can be described as a function of temperature, $E=3 / 2 n R T$, where $n=1$ mole. Therefore, the internal energy at $15^{\circ} \mathrm{C}$ and $30^{\circ} \mathrm{C}$ can be calculated. The inside back cover lists values of $R$ with different units.
$E=3 / 2 n R T=(3 / 2)(1.00 \mathrm{~mol})(8.314 \mathrm{~J} / \mathrm{mol} \cdot \mathrm{K})(303-288) \mathrm{K}=187.065=\mathbf{1 8 7} \mathbf{J}$
c) When the balloon expands as temperature rises, the balloon performs $P V$ work. However, the problem specifies that pressure remains constant, so work done on the surroundings by the balloon is defined by the equation: $w=-P \Delta V$. When pressure and volume are multiplied together, the unit is $L \cdot a t m$, so a conversion factor is needed to convert work in units of $L \cdot a t m$ to joules.
$w=-P \Delta V=-(1.00 \mathrm{~atm})((24.8763-23.6448) \mathrm{L})\left(\frac{101.3 \mathrm{~J}}{1 \mathrm{~L} \cdot \mathrm{~atm}}\right)=-124.75=-\mathbf{1 . 2 \times 1 0 ^ { 2 }} \mathbf{J}$
d) $q_{P}=\Delta E+P \Delta V=(187.065 \mathrm{~J})+(124.75 \mathrm{~J})=311.815=\mathbf{3 . 1} \mathbf{x 1 0} \mathbf{0}^{2} \mathbf{J}$
e) $\Delta H=q_{P}=310 \mathrm{~J}$.
f) When a process occurs at constant pressure, the change in heat energy of the system can be described by a state function called enthalpy. The change in enthalpy equals the heat $(q)$ lost at constant pressure: $\Delta H=\Delta E+P \Delta V=$ $\Delta E-w=(q+w)-w=q_{P}$
a) Respiration:
$\mathrm{C}_{6} \mathrm{H}_{12} \mathrm{O}_{6}(\mathrm{~s})+6 \mathrm{O}_{2}(\mathrm{~g}) \rightarrow 6 \mathrm{CO}_{2}(\mathrm{~g})+6 \mathrm{H}_{2} \mathrm{O}(\mathrm{g})$
$\Delta H_{\mathrm{rxn}}^{\circ}=\sum m \Delta H_{\mathrm{f}}^{\circ}$ (products) $-\sum n \Delta H_{\mathrm{f}}^{\circ}$ (reactants)

$$
\begin{aligned}
& =\left\{6 \Delta H_{\mathrm{f}}^{\circ}\left[\mathrm{CO}_{2}(\mathrm{~g})\right]+6 \Delta H_{\mathrm{f}}^{\circ}\left[\mathrm{H}_{2} \mathrm{O}(\mathrm{~g})\right]\right\}-\left\{1 \Delta H_{\mathrm{f}}^{\circ}\left[\mathrm{C}_{6} \mathrm{H}_{12} \mathrm{O}_{6}(\mathrm{~s})\right]+6 \Delta H_{\mathrm{f}}^{\circ}\left[\mathrm{O}_{2}(\mathrm{~g})\right]\right\} \\
& =[(6 \mathrm{~mol})(-393.5 \mathrm{~kJ} / \mathrm{mol})+(6 \mathrm{~mol})(-241.826 \mathrm{~kJ} / \mathrm{mol})]-[(1 \mathrm{~mol})(-1273.3 \mathrm{~kJ} / \mathrm{mol})+(6 \mathrm{~mol})(0.0 \mathrm{~kJ} / \mathrm{mol})] \\
& =-2538.656=-2538.7 \mathbf{k J}
\end{aligned}
$$

Fermentation:
$\mathrm{C}_{6} \mathrm{H}_{12} \mathrm{O}_{6}(\mathrm{~s}) \rightarrow 2 \mathrm{CO}_{2}(\mathrm{~g})+2 \mathrm{CH}_{3} \mathrm{CH}_{2} \mathrm{OH}(\mathrm{l})$
$\Delta H_{\mathrm{rxn}}^{\circ}=\left\{2 \Delta H_{\mathrm{f}}^{\circ}\left[\mathrm{CO}_{2}(\mathrm{~g})\right]+2 \Delta H_{\mathrm{f}}^{\circ}\left[\mathrm{CH}_{3} \mathrm{CH}_{2} \mathrm{OH}(\mathrm{l})\right]\right\}-\left[1 \Delta H_{\mathrm{f}}^{\circ}\left[\mathrm{C}_{6} \mathrm{H}_{12} \mathrm{O}_{6}(\mathrm{~s})\right]\right\}$

$$
=[(2 \mathrm{~mol})(-393.5 \mathrm{~kJ} / \mathrm{mol})+(2 \mathrm{~mol})(-277.63 \mathrm{~kJ} / \mathrm{mol})]-[(1 \mathrm{~mol})(-1273.3 \mathrm{~kJ} / \mathrm{mol})]=-68.96=-\mathbf{6 9 . 0} \mathbf{~ k J}
$$

b) Combustion of ethanol:
$\mathrm{CH}_{3} \mathrm{CH}_{2} \mathrm{OH}(\mathrm{l})+3 \mathrm{O}_{2}(\mathrm{~g}) \rightarrow 2 \mathrm{CO}_{2}(\mathrm{~g})+3 \mathrm{H}_{2} \mathrm{O}(\mathrm{g})$
$\Delta H_{\mathrm{rxn}}^{\circ}=\left\{2 \Delta H_{\mathrm{f}}^{\circ}\left[\mathrm{CO}_{2}(\mathrm{~g})\right]+3 \Delta H_{\mathrm{f}}^{\circ}\left[\mathrm{H}_{2} \mathrm{O}(\mathrm{g})\right]\right\}-\left\{1 \Delta H_{\mathrm{f}}^{\circ}\left[\mathrm{CH}_{3} \mathrm{CH}_{2} \mathrm{OH}(\mathrm{l})\right]+3 \Delta H_{\mathrm{f}}^{\circ}\left[\mathrm{O}_{2}(\mathrm{~g})\right]\right\}$

$$
\begin{aligned}
\Delta H_{\mathrm{rxn}}^{\circ} & =[(2 \mathrm{~mol})(-393.5 \mathrm{~kJ} / \mathrm{mol})+(3 \mathrm{~mol})(-241.826 \mathrm{~kJ} / \mathrm{mol})]-[(1 \mathrm{~mol})(-277.63 \mathrm{~kJ} / \mathrm{mol})+(3 \mathrm{~mol})(0.0 \mathrm{~kJ} / \mathrm{mol})] \\
& =-1234.848=-1234.8 \mathbf{~ k J}
\end{aligned}
$$

Heats of combustion/mol C:
Sugar: $\left(\frac{-2538.656 \mathrm{~kJ}}{1 \mathrm{~mol} \mathrm{C}_{6} \mathrm{H}_{12} \mathrm{O}_{6}}\right)\left(\frac{1 \mathrm{~mol} \mathrm{C}_{6} \mathrm{H}_{12} \mathrm{O}_{6}}{6 \mathrm{~mol} \mathrm{C}}\right)=-423.1093=-423.11 \mathrm{~kJ} / \mathrm{mol} \mathrm{C}$
Ethanol: $\left(\frac{-1234.848 \mathrm{~kJ}}{1 \mathrm{~mol} \mathrm{CH}_{3} \mathrm{CH}_{2} \mathrm{OH}}\right)\left(\frac{1 \mathrm{~mol} \mathrm{CH}_{3} \mathrm{CH}_{2} \mathrm{OH}}{2 \mathrm{~mol} \mathrm{C}}\right)=-617.424=-617.42 \mathrm{~kJ} / \mathrm{mol} \mathrm{C}$
Ethanol has a higher value.
a)

$$
=-2.585869657 \times 10^{6}=-\mathbf{2 . 5 9 \times 1 0 ^ { 6 }} \mathbf{k J}
$$

b) Miles $=\left(-2.585869657 \times 10^{6} \mathrm{~kJ}\right)\left(\frac{1 \mathrm{~h}}{-5.5 \times 10^{4} \mathrm{~kJ}}\right)\left(\frac{65 \mathrm{mi}}{1 \mathrm{~h}}\right)\left(\frac{1 \mathrm{~km}}{0.62 \mathrm{mi}}\right)=4929.1=4.9 \times 10^{3} \mathbf{~ k m}$
c) Only a small percentage of the chemical energy in the fuel is converted to work to move the car; most of the chemical energy is lost as waste heat flowing into the surroundings.
$q=c \times$ mass $\times \Delta T$
In this situation, all of the samples have the same mass, $50 . \mathrm{g}$, so mass is not a variable.
All also have the same $q$ value, 450. J. So, 450. J $\alpha(c \times \Delta T)$. $c$, specific heat capacity, and $\Delta T$ are inversely proportional. The higher the $\Delta T$, the lower the value of specific heat capacity:
$\Delta T: \mathrm{B}>\mathrm{D}>\mathrm{C}>\mathrm{A}$
Specific heat capacity: $\mathbf{B}<\mathbf{D}<\mathbf{C}<\mathbf{A}$
$\mathrm{C}_{6} \mathrm{H}_{12} \mathrm{O}_{6}(s)+\mathrm{C}_{6} \mathrm{H}_{12} \mathrm{O}_{6}(s) \rightarrow \mathrm{C}_{12} \mathrm{H}_{22} \mathrm{O}_{11}(s)+\mathrm{H}_{2} \mathrm{O}(l)$
$\Delta H_{\mathrm{rxn}}^{\circ}=[(1 \mathrm{~mol}$ sucrose $)(-2226 \mathrm{~kJ} / \mathrm{mol})+(1 \mathrm{~mol} \mathrm{H} \mathrm{O})(-285.840 \mathrm{~kJ} / \mathrm{mol})]-[(1 \mathrm{~mol}$ glucose $)(-1273 \mathrm{~kJ} / \mathrm{mol})$ + (1 mol fructose)( $-1266 \mathrm{~kJ} / \mathrm{mol})]=\mathbf{2 7} \mathbf{~ k J} / \mathbf{m o l}$ sucrose
6.67
a) $3 \mathrm{~N}_{2} \mathrm{O}_{5}(g)+3 \mathrm{NO}(g) \rightarrow 9 \mathrm{NO}_{2}(g)$
$\Delta H_{\mathrm{rxn}}^{\circ}=\left\{9 \Delta H_{\mathrm{f}}^{\circ}\left[\mathrm{NO}_{2}(\mathrm{~g})\right]\right\}-\left\{3 \Delta H_{\mathrm{f}}^{\circ}\left[\mathrm{N}_{2} \mathrm{O}_{5}(\mathrm{~g})\right]+3 \Delta H_{\mathrm{f}}^{\circ}[\mathrm{NO}(\mathrm{g})]\right\}$ $=[(9 \mathrm{~mol})(33.2 \mathrm{~kJ} / \mathrm{mol})]-[(3 \mathrm{~mol})(11 \mathrm{~kJ} / \mathrm{mol})+(3 \mathrm{~mol})(90.29 \mathrm{~kJ} / \mathrm{mol})]$ $=-5.07=-5 \mathbf{k J}$
b) $(9$ molecules product $)\left(\frac{1.50 \times 10^{-2} \mathrm{~mol}}{1 \text { molecule product }}\right)\left(\frac{-5.07 \mathrm{~kJ}}{9 \text { moles product }}\right)\left(\frac{10^{3} \mathrm{~J}}{1 \mathrm{~kJ}}\right)=-76.05=-76.0 \mathrm{~J}$
b) $\quad \mathrm{Fe}_{2} \mathrm{O}_{3}(s)+1 / 3 \mathrm{CO}(g) \rightarrow 2 / 3 \mathrm{Fe}_{3} \mathrm{O}_{4}(\mathrm{~s})+1 / 3 \mathrm{CO}_{2}(g)$

Total: $\quad \mathrm{Fe}_{2} \mathrm{O}_{3}(\mathrm{~s})+3 \mathrm{CO}(\mathrm{g}) \rightarrow 2 \mathrm{Fe}(\mathrm{s})+3 \mathrm{CO}_{2}(\mathrm{~g})$
a) Heat $=(20.4 \mathrm{gal})\left(\frac{4 \mathrm{qt}}{1 \mathrm{gal}}\right)\left(\frac{1 \mathrm{~L}}{1.057 \mathrm{qt}}\right)\left(\frac{1 \mathrm{~mL}}{10^{-3} \mathrm{~L}}\right)\left(\frac{0.702 \mathrm{~g}}{\mathrm{~mL}}\right)\left(\frac{1 \mathrm{~mol} \mathrm{C}_{8} \mathrm{H}_{18}}{114.22 \mathrm{~g}}\right)\left(\frac{-5.45 \mathrm{x} \mathrm{10}^{3} \mathrm{~kJ}}{1 \mathrm{~mol} \mathrm{C}_{8} \mathrm{H}_{18}}\right)$
$\Delta H^{\circ}=1 / 3(-48.5 \mathrm{~kJ})=-16.2 \mathrm{~kJ}$
$\Delta H^{\circ}=-2(-11.0 \mathrm{~kJ})=22.0 \mathrm{~kJ}$
$\Delta H^{\circ}=2 / 3(22 \mathrm{~kJ})=14.7 \mathrm{~kJ}$
$\Delta H_{\mathrm{rxn}}^{\circ}=\quad 21 \mathrm{~kJ}$
6.70 Plan: Chemical equations can be written that describe the three processes. Assume one mole of each substance of interest so that units are expressed as kJ . To obtain the overall reaction, reverse the third reaction and multiply its coefficients by two and add to the first two reactions. When the third reaction is reversed, the sign of its enthalpy change is reversed from positive to negative.
Solution:
(1) C (graphite) $+2 \mathrm{H}_{2}(g) \rightarrow \mathrm{CH}_{4}(g)$
(2) $\mathrm{CH}_{4}(g) \rightarrow \mathrm{C}(g)+4 \mathrm{H}(g)$

$$
\Delta H_{\mathrm{f}}^{\circ}=\Delta H_{\mathrm{rxn}}^{\circ}=-74.9 \mathrm{~kJ}
$$

$$
\Delta H_{\mathrm{atom}}^{\circ}=\Delta H_{\mathrm{rxn}}^{\circ}=1660 \mathrm{~kJ}
$$

(3) $\mathrm{H}_{2}(g) \rightarrow 2 \mathrm{H}(g)$
$\Delta H_{\text {atom }}^{\circ}=\Delta H_{\mathrm{rxn}}^{\circ}=432 \mathrm{~kJ}$
The third equation is reversed and its coefficients are multiplied by 2 to add the three equations.

| C (graphite) $+2 \mathrm{H}_{2}(\mathrm{~g}) \rightarrow \mathrm{CH}_{4}(\mathrm{~g})$ | $\Delta H_{\text {rxn }}^{\circ}=-74.9 \mathrm{~kJ}$ |
| :---: | :---: |
| $\mathrm{CH}_{4}(\mathrm{~g}) \rightarrow \mathrm{C}(\mathrm{g})+4 \mathrm{H}(\mathrm{g})$ | $\Delta H_{\mathrm{rxn}}^{\circ}=1660 \mathrm{~kJ}$ |
| $4 \mathrm{H}(\mathrm{g}) \rightarrow 2 \mathrm{H}_{2}(\mathrm{~g})$ | $\Delta H_{\mathrm{rxn}}^{\circ}=-2(432 \mathrm{~kJ})=-864 \mathrm{~kJ}$ |
| C(graphite) $\rightarrow \mathrm{C}(\mathrm{g})$ | $\Delta H_{\mathrm{rxn}}^{\circ}=\Delta H_{\mathrm{atom}}^{\circ}=721.1=721 \mathbf{k J}$ per one mol C(graphite) |

6.71 The reaction is exothermic. The argon atoms in the chamber after the reaction are moving with greater kinetic energy, indicating an increase in temperature.

Plan: Write balanced chemical equations for the combustion reactions and use the standard heats of formation to determine the energy released.
Solution:

$$
\begin{aligned}
& \mathrm{C}_{6} \mathrm{H}_{6}(\mathrm{~g})+15 / 2 \mathrm{O}_{2}(\mathrm{~g}) \rightarrow 6 \mathrm{CO}_{2}(\mathrm{~g})+3 \mathrm{H}_{2} \mathrm{O}(\mathrm{~g}) \\
& \Delta H_{\mathrm{rxn}}^{\circ}=\left\{6 \Delta H_{\mathrm{f}}^{\circ}\left[\mathrm{CO}_{2}(\mathrm{~g})\right]+3 \Delta H_{\mathrm{f}}^{\circ}\left[\mathrm{H}_{2} \mathrm{O}(\mathrm{~g})\right]\right\}-\left\{1 \Delta H_{\mathrm{f}}^{\circ}\left[\mathrm{C}_{6} \mathrm{H}_{6}(\mathrm{~g})\right]+15 / 2 \Delta H_{\mathrm{f}}^{\circ}\left[\mathrm{O}_{2}(\mathrm{~g})\right]\right\} \\
& \Delta H_{\mathrm{rxn}}^{\circ}=[(6 \mathrm{~mol})(-393.5 \mathrm{~kJ} / \mathrm{mol})+(3 \mathrm{~mol})(-241.826 \mathrm{~kJ} / \mathrm{mol})]-[(1 \mathrm{~mol})(82.9 \mathrm{~kJ} / \mathrm{mol})+(15 / 2 \mathrm{~mol})(0.0 \mathrm{~kJ} / \mathrm{mol})] \\
& =-3169.378 \\
& \Delta H_{\mathrm{rxn}}^{\circ} \text { per mole of } \mathrm{CH}=\left(\frac{-3169.378 \mathrm{~kJ}}{\mathrm{~mol} \mathrm{C}_{6} \mathrm{H}_{6}}\right)\left(\frac{1 \mathrm{~mol} \mathrm{C}_{6} \mathrm{H}_{6}}{6 \mathrm{~mol} \mathrm{CH}}\right)=-528.2297=-\mathbf{5 2 8 . 2} \mathbf{~ k J} / \mathbf{m o l} \mathbf{C H} \\
& \mathrm{C}_{2} \mathrm{H}_{2}(\mathrm{~g})+5 / 2 \mathrm{O}_{2}(\mathrm{~g}) \rightarrow 2 \mathrm{CO}_{2}(\mathrm{~g})+\mathrm{H}_{2} \mathrm{O}(\mathrm{~g}) \\
& \Delta H_{\mathrm{rxn}}^{\circ}=\left\{2 \Delta H_{\mathrm{f}}^{\circ}\left[\mathrm{CO}_{2}(\mathrm{~g})\right]+1\left[\Delta H_{\mathrm{f}}^{\circ}\left[\mathrm{H}_{2} \mathrm{O}(\mathrm{~g})\right]\right\}-\left\{1 \Delta H_{\mathrm{f}}^{\circ}\left[\mathrm{C}_{2} \mathrm{H}_{2}(\mathrm{~g})\right]+5 / 2 \Delta H_{\mathrm{f}}^{\circ}\left[\mathrm{O}_{2}(\mathrm{~g})\right]\right\}\right. \\
& \Delta H_{\mathrm{rxn}}^{\circ}=[(2 \mathrm{~mol})(-393.5 \mathrm{~kJ} / \mathrm{mol})+(1 \mathrm{~mol})(-241.826 \mathrm{~kJ} / \mathrm{mol})]-[(1 \mathrm{~mol})(227 \mathrm{~kJ} / \mathrm{mol})+(5 / 2 \mathrm{~mol})(0.0 \mathrm{~kJ} / \mathrm{mol})] \\
& =-1255.826 \mathrm{~kJ} \\
& \Delta H_{\mathrm{rxn}}^{\circ} \text { per mole of } \mathrm{CH}=\left(\frac{-1255.826 \mathrm{~kJ}}{\mathrm{~mol} \mathrm{C}_{2} \mathrm{H}_{2}}\right)\left(\frac{1 \mathrm{~mol} \mathrm{C}_{2} \mathrm{H}_{2}}{2 \mathrm{~mol} \mathrm{CH}}\right)=-627.913=-\mathbf{6 2 8} \mathbf{~ k J} / \mathbf{m o l ~ C H}
\end{aligned}
$$

Thus, acetylene releases more energy per CH than benzene does.
$6.73 \quad \mathrm{H}_{2} \mathrm{SO}_{4}(a q)+2 \mathrm{NaOH}(a q) \rightarrow \mathrm{Na}_{2} \mathrm{SO}_{4}(a q)+2 \mathrm{H}_{2} \mathrm{O}(l)$
$2 \mathrm{H}^{+}(a q)+2 \mathrm{OH}^{-}(a q) \rightarrow 2 \mathrm{H}_{2} \mathrm{O}(l)$
$\Delta H_{\mathrm{rxn}}^{\circ}=\left\{2 \Delta H_{\mathrm{f}}^{\circ}\left[\mathrm{H}_{2} \mathrm{O}(\mathrm{l})\right]\right\}-\left\{2 \Delta H_{\mathrm{f}}^{\circ}\left[\mathrm{H}^{+}(a q)\right]+2 \Delta H_{\mathrm{f}}^{\circ}\left[\mathrm{OH}^{-}(a q)\right]\right\}$
$=[(2 \mathrm{~mol})(-285.84 \mathrm{~kJ} / \mathrm{mol})]-[(2 \mathrm{~mol})(0 \mathrm{~kJ} / \mathrm{mol})+(2 \mathrm{~mol})(-229.94 \mathrm{~kJ} / \mathrm{mol})]$

$$
=-111.8 \mathrm{~kJ}
$$

1 mole of $\mathrm{H}_{2} \mathrm{SO}_{4}$ reacts with 2 moles of NaOH .
Mass (g) of $\mathrm{H}_{2} \mathrm{SO}_{4}$ solution $=\left(1 \mathrm{~mol} \mathrm{H}_{2} \mathrm{SO}_{4}\right)\left(\frac{1.00 \mathrm{~L}}{0.50 \mathrm{~mol} \mathrm{H}_{2} \mathrm{SO}_{4}}\right)\left(\frac{1.00 \mathrm{~mL}}{10^{-3} \mathrm{~L}}\right)\left(\frac{1.030 \mathrm{~g}}{1.00 \mathrm{~mL}}\right)$

$$
=2060 \mathrm{~g} \mathrm{H}_{2} \mathrm{SO}_{4} \text { solution }
$$

Mass $(\mathrm{g})$ of NaOH solution $=(2 \mathrm{~mol} \mathrm{NaOH})\left(\frac{40.00 \mathrm{~g} \mathrm{NaOH}}{1 \mathrm{~mol} \mathrm{NaOH}}\right)\left(\frac{100 \mathrm{~g} \text { solution }}{40 \mathrm{~g} \mathrm{NaOH}}\right)=200 . \mathrm{g} \mathrm{NaOH}$ solution $q=c \times$ mass $\times \Delta T$

$$
\begin{aligned}
& \Delta T=\frac{q}{c \text { x mass }}=\frac{(111.8 \mathrm{~kJ})\left(\frac{10^{3} \mathrm{~J}}{1 \mathrm{~kJ}}\right)}{4.184 \mathrm{~J} / \mathrm{g}^{\circ} \mathrm{C}((2060+200) \mathrm{g})}=11.82^{\circ} \mathrm{C} \\
& 31^{\circ} \mathrm{C}+11.82^{\circ} \mathrm{C}=42.82=43^{\circ} \mathrm{C}
\end{aligned}
$$

This temperature is above the temperature at which a flammable vapor could be formed so the temperature increase could cause the vapor to explode.
a) $2 \mathrm{C}_{12} \mathrm{H}_{26}(\mathrm{l})+37 \mathrm{O}_{2}(\mathrm{~g}) \rightarrow 24 \mathrm{CO}_{2}(\mathrm{~g})+26 \mathrm{H}_{2} \mathrm{O}(\mathrm{g})$
b) $\Delta H_{\mathrm{rxn}}^{\circ}=\left\{24 \Delta H_{\mathrm{f}}^{\circ}\left[\mathrm{CO}_{2}(\mathrm{~g})\right]+26 \Delta H_{\mathrm{f}}^{\circ}\left[\mathrm{H}_{2} \mathrm{O}(\mathrm{g})\right]\right\}-\left\{2 \Delta H_{\mathrm{f}}^{\circ}\left[\mathrm{C}_{12} \mathrm{H}_{26}(\mathrm{~g})\right]+37 \Delta H_{\mathrm{f}}^{\circ}\left[\mathrm{O}_{2}(\mathrm{~g})\right]\right\}$
$-1.50 \times 10^{4} \mathrm{~kJ}=[(24 \mathrm{~mol})(-393.5 \mathrm{~kJ} / \mathrm{mol})+(26 \mathrm{~mol})(-241.826 \mathrm{~kJ} / \mathrm{mol})]$
$-\left[(2 \mathrm{~mol}) \Delta H_{\mathrm{f}}^{\circ}\left[\mathrm{C}_{12} \mathrm{H}_{26}(\mathrm{~g})\right]+(37 \mathrm{~mol})(0.0 \mathrm{~kJ} / \mathrm{mol})\right]$
$-1.50 \times 10^{4} \mathrm{~kJ}=-9444.0 \mathrm{~kJ}+-6287.476 \mathrm{~kJ}-\left[(2 \mathrm{~mol}) \Delta H_{\mathrm{f}}^{\circ}\left[\mathrm{C}_{12} \mathrm{H}_{26}(g)\right]+0.0 \mathrm{~kJ}\right]$
$-1.50 \times 10^{4} \mathrm{~kJ}=-15,731.476 \mathrm{~kJ}-(2 \mathrm{~mol}) \Delta H_{\mathrm{f}}^{\circ}\left[\mathrm{C}_{12} \mathrm{H}_{26}(\mathrm{~g})\right]$
$-1.50 \times 10^{4} \mathrm{~kJ}+15,731.476 \mathrm{~kJ}=-(2 \mathrm{~mol}) \Delta H_{\mathrm{f}}^{\circ}\left[\mathrm{C}_{12} \mathrm{H}_{26}(\mathrm{~g})\right]$
$731.476 \mathrm{~kJ}=-(2 \mathrm{~mol}) \Delta H_{\mathrm{f}}^{\circ}\left[\mathrm{C}_{12} \mathrm{H}_{26}(\mathrm{~g})\right]$
$\Delta H_{\mathrm{f}}^{\circ}\left[\mathrm{C}_{12} \mathrm{H}_{26}(\mathrm{~g})\right]=-365.738=-\mathbf{3 . 6 6 \times 1 0} \mathbf{0}^{\mathbf{2}} \mathbf{k J}$
c) Heat $(\mathrm{kJ})=(0.50 \mathrm{gal})\left(\frac{4 \mathrm{qt}}{1 \mathrm{gal}}\right)\left(\frac{1 \mathrm{~L}}{1.057 \mathrm{qt}}\right)\left(\frac{1 \mathrm{~mL}}{10^{-3} \mathrm{~L}}\right)\left(\frac{0.749 \mathrm{~g} \mathrm{C}_{12} \mathrm{H}_{26}}{\mathrm{~mL}}\right)\left(\frac{1 \mathrm{~mol} \mathrm{C}_{12} \mathrm{H}_{26}}{170.33 \mathrm{~g} \mathrm{C}_{12} \mathrm{H}_{26}}\right)\left(\frac{-1.50 \mathrm{x} 10^{4} \mathrm{~kJ}}{2 \mathrm{~mol} \mathrm{C}_{12} \mathrm{H}_{26}}\right)$

$$
=-6.2403 \times 10^{4}=-6.2 \times 10^{4} \mathbf{k J}
$$

d) Volume (gal) $=(1250$. Btu $)\left(\frac{1.055 \mathrm{~kJ}}{1 \mathrm{Btu}}\right)\left(\frac{0.50 \mathrm{gal}}{6.2403 \times 10^{4} \mathrm{~kJ}}\right)=0.010566=\mathbf{1 . 1 \times 1 0 ^ { - 2 }} \mathbf{~ g a l}$
6.75 Use Hess's Law:

$$
\text { a) } \begin{array}{ll}
\text { 1) } \mathrm{C}(\text { coal })+\mathrm{H}_{2} \mathrm{O}(g) \rightarrow \mathrm{CO}(g)+\mathrm{H}_{2}(g) & \Delta H_{\mathrm{rxn}}^{\circ}=129.7 \mathrm{~kJ} \\
\text { 2) } \mathrm{CO}(g)+\mathrm{H}_{2} \mathrm{O}(g) \rightarrow \mathrm{CO}_{2}(g)+\mathrm{H}_{2}(g) & \Delta H_{\mathrm{rxn}}^{\circ}=-41 \mathrm{~kJ} \\
\text { 3) } \mathrm{CO}(g)+3 \mathrm{H}_{2}(g) \rightarrow \mathrm{CH}_{4}(g)+\mathrm{H}_{2} \mathrm{O}(g) & \Delta H_{\mathrm{rxn}}^{\circ}=-206 \mathrm{~kJ}
\end{array}
$$

Equation 1) must be multiplied by 2 and then the reactions are added:

$$
\begin{array}{ll}
\text { 1) } 2 \mathrm{C}(\text { coal })+2 \mathrm{H}_{2} \mathrm{O}(g) \rightarrow 2 \mathrm{CO}(g)+2 \mathrm{H}_{2}(g) & \Delta H_{\mathrm{rxn}}^{\circ}=2(129.7 \mathrm{~kJ}) \\
\text { 2) } \mathrm{GO}(\mathrm{~g})+\mathrm{H}_{z} \mathrm{O}(g) \rightarrow \mathrm{CO}_{2}(\mathrm{~g})+\mathrm{H}_{z}(g) & \Delta H_{\mathrm{rxn}}^{\circ}=-41 \mathrm{~kJ} \\
\text { 3) } \mathrm{CO}(g)+3 \mathrm{H}_{2}(g) \rightarrow \mathrm{CH}_{4}(g)+\mathrm{H}_{2} \mathrm{O}(g) & \Delta H_{\mathrm{rxn}}^{\circ}=-206 \mathrm{~kJ} \\
\hline \text { 2C(coal })+2 \mathrm{H}_{2} \mathrm{O}(g) \rightarrow \mathrm{CH}_{4}(g)+\mathrm{CO}_{2}(g) &
\end{array}
$$

b) The total may be determined by doubling the value for equation 1) and adding to the other two values.

$$
\Delta H_{\mathrm{rxn}}^{\circ}=2(129.7 \mathrm{~kJ})+(-41 \mathrm{~kJ})+(-206 \mathrm{~kJ})=12.4=\mathbf{1 2} \mathbf{~ k J}
$$

c) Calculating the heat of combustion of $\mathrm{CH}_{4}$ :

$$
\begin{aligned}
& \mathrm{CH}_{4}(\mathrm{~g})+2 \mathrm{O}_{2}(\mathrm{~g}) \rightarrow \mathrm{CO}_{2}(\mathrm{~g})+2 \mathrm{H}_{2} \mathrm{O}(\mathrm{~g}) \\
& \left.\Delta H_{\text {comb }}^{\circ}=\left\{1 \Delta H_{\mathrm{f}}^{\circ}\left[\mathrm{CO}_{2}(\mathrm{~g})\right]+2 \Delta H_{\mathrm{f}}^{\circ}\left[\mathrm{H}_{2} \mathrm{O}(\mathrm{~g})\right]\right\}-\left\{1 \Delta H_{\mathrm{f}}^{\circ}\left[\mathrm{CH}_{4}(\mathrm{~g})\right]\right\}-2 \Delta H_{\mathrm{f}}^{\circ}\left[\mathrm{O}_{2}(\mathrm{~g})\right]\right\} \\
& \Delta H_{\text {comb }}^{\circ}=[(1 \mathrm{~mol})(-395.5 \mathrm{~kJ} / \mathrm{mol})+(2 \mathrm{~mol})(-241.826 \mathrm{~kJ} / \mathrm{mol})] \\
& -[(1 \mathrm{~mol})(-74.87 \mathrm{~kJ} / \mathrm{mol})-(2 \mathrm{~mol})(0.0 \mathrm{~kJ} / \mathrm{mol})] \\
& =-804.282 \mathrm{~kJ} / \mathrm{mol} \mathrm{CH}_{4}
\end{aligned}
$$

Total heat for gasification of 1.00 kg coal:

$$
\Delta H^{\circ}=(1.00 \mathrm{~kg} \text { coal })\left(\frac{10^{3} \mathrm{~g}}{1 \mathrm{~kg}}\right)\left(\frac{1 \mathrm{~mol} \mathrm{coal}}{12.00 \mathrm{~g} \mathrm{coal}}\right)\left(\frac{12.4 \mathrm{~kJ}}{2 \mathrm{~mol} \mathrm{coal}}\right)=516.667 \mathrm{~kJ}
$$

Total heat from burning the methane formed from 1.00 kg of coal:

$$
\begin{aligned}
\Delta H^{\circ} & =(1.00 \mathrm{~kg} \text { coal })\left(\frac{10^{3} \mathrm{~g}}{1 \mathrm{~kg}}\right)\left(\frac{1 \mathrm{~mol} \mathrm{coal}}{12.00 \mathrm{~g} \mathrm{coal}}\right)\left(\frac{1 \mathrm{~mol} \mathrm{CH}_{4}}{2 \mathrm{~mol} \mathrm{coal}}\right)\left(\frac{-804.282 \mathrm{~kJ}}{1 \mathrm{~mol} \mathrm{CH}_{4}}\right) \\
& =-33511.75 \mathrm{~kJ}
\end{aligned}
$$

Total heat $=516.667 \mathrm{~kJ}-33511.75 \mathrm{~kJ}=32995.083=\mathbf{3 . 3 0} \mathbf{x 1 0} \mathbf{~ k J}$

|  | $\mathrm{PCl}_{3}(\mathrm{~g}) \rightarrow 1 / 4 \mathrm{P}_{4}(\mathrm{~s})+3 / 2 \mathrm{Cl}_{2}(\mathrm{~g})$ | $\Delta H=-1 / 4(-1280 \mathrm{~kJ})=320 \mathrm{~kJ}$ |
| :---: | :---: | :---: |
|  | $1 / 4 \mathrm{P}_{4}(\mathrm{~s})+5 / 2 \mathrm{Cl}_{2}(\mathrm{~g}) \rightarrow \mathrm{PCl}_{5}(\mathrm{~g})$ | $\Delta H=1 / 4(-1774 \mathrm{~kJ})=-443.5 \mathrm{~kJ}$ |
| Total: | $\mathrm{PCl}_{3}(\mathrm{~g})+\mathrm{Cl}_{2}(\mathrm{~g}) \rightarrow \mathrm{PCl}_{5}(\mathrm{~g})$ | $\Delta H=-123.5=\mathbf{1 2 4} \mathbf{~ k J}$ |

a) Energy $(\mathrm{kJ})=(2 \mathrm{oz})\left(\frac{28.4 \mathrm{~g}}{1.00 \mathrm{oz}}\right)\left(\frac{4.0 \mathrm{Cal}}{1.0 \mathrm{~g}}\right)\left(\frac{1 \mathrm{kcal}}{1 \mathrm{Cal}}\right)\left(\frac{4.184 \mathrm{~kJ}}{1 \mathrm{kcal}}\right)=950.60=\mathbf{1} \times \mathbf{1 0}^{\mathbf{3}} \mathbf{~ k J}$
b) Energy $=E=$ mass $\mathrm{x} g \times$ height $=m g h$

$$
h=\frac{E}{m g}=\frac{(950.60 \mathrm{~kJ})}{(58 \mathrm{~kg})\left(9.8 \mathrm{~m} / \mathrm{s}^{2}\right)}\left(\frac{10^{3} \mathrm{~J}}{1 \mathrm{~kJ}}\right)\left(\frac{\mathrm{kg} \cdot \mathrm{~m}^{2} / \mathrm{s}^{2}}{\mathrm{~J}}\right)=1672.41=2 \times 10^{3} \mathrm{~m}
$$

c) Energy is also converted to heat.
6.78

Plan: Heat of reaction is calculated using the relationship $\Delta H_{\mathrm{rxn}}^{\circ}=\sum m \Delta H_{\mathrm{f}}^{\circ}$ (products) $-\sum n \Delta H_{\mathrm{f}}^{\circ}$ (reactants) . The heats of formation for all of the species, except $\mathrm{SiCl}_{4}$, are found in Appendix B. Use reaction 3, with its given $\Delta H_{\mathrm{rxn}}^{\circ}$, to find the heat of formation of $\mathrm{SiCl}_{4}(\mathrm{~g})$. Once the heat of formation of $\mathrm{SiCl}_{4}$ is known, the heat of reaction of the other two reactions can be calculated. When reactions 2 and 3 are added to obtain a fourth reaction, the heats of reaction of reactions 2 and 3 are also added to obtain the heat of reaction for the fourth reaction.
Solution:
a) (3) $\mathrm{SiCl}_{4}(g)+2 \mathrm{H}_{2} \mathrm{O}(g) \rightarrow \mathrm{SiO}_{2}(s)+4 \mathrm{HCl}(g)$

$$
\begin{aligned}
& \Delta H_{\mathrm{rxn}}^{\circ}=\left\{1 \Delta H_{\mathrm{f}}^{\circ}\left[\mathrm{SiO}_{2}(\mathrm{~s})\right]+4 \Delta H_{\mathrm{f}}^{\circ}[\mathrm{HCl}(\mathrm{~g})]\right\}-\left\{1 \Delta H_{\mathrm{f}}^{\circ}\left[\mathrm{SiCl}_{4}(\mathrm{~g})\right]+2 \Delta H_{\mathrm{f}}^{\circ}\left[\mathrm{H}_{2} \mathrm{O}(\mathrm{~g})\right]\right\} \\
& -139.5 \mathrm{~kJ}=[(1 \mathrm{~mol})(-910.9 \mathrm{~kJ} / \mathrm{mol})+(4 \mathrm{~mol})(-92.31 \mathrm{~kJ} / \mathrm{mol})]-\left[\Delta H_{\mathrm{f}}^{\circ}\left[\mathrm{SiCl}_{4}(\mathrm{~g})\right]+(2 \mathrm{~mol})(-241.826 \mathrm{~kJ} / \mathrm{mol})\right] \\
& -139.5 \mathrm{~kJ}=-1280.14-\left[\Delta H_{\mathrm{f}}^{\circ}\left[\mathrm{SiCl}_{4}(\mathrm{~g})\right]+(-483.652 \mathrm{~kJ})\right] \\
& 1140.64 \mathrm{~kJ}=-\Delta H_{\mathrm{f}}^{\circ}\left[\mathrm{SiCl}_{4}(\mathrm{~g})\right]+483.652 \mathrm{~kJ}
\end{aligned}
$$

$\Delta H_{\mathrm{f}}^{\circ}\left[\mathrm{SiCl}_{4}(\mathrm{~g})\right]=-656.988 \mathrm{~kJ} / \mathrm{mol}$
The heats of reaction for the first two steps can now be calculated.

1) $\mathrm{Si}(s)+2 \mathrm{Cl}_{2}(g) \rightarrow \mathrm{SiCl}_{4}(g)$

$$
\begin{aligned}
& \Delta H_{\mathrm{rxn}}^{\circ}=\left\{1 \Delta H_{\mathrm{f}}^{\circ}\left[\mathrm{SiCl}_{4}(g)\right]\right\}-\left\{1 \Delta H_{\mathrm{f}}^{\circ}[\mathrm{Si}(\mathrm{~s})]+2 \Delta H_{\mathrm{f}}^{\circ}\left[\mathrm{Cl}_{2}(g)\right]\right\} \\
&= {[(1 \mathrm{~mol})(-656.988 \mathrm{~kJ} / \mathrm{mol})]-[(1 \mathrm{~mol})(0 \mathrm{~kJ} / \mathrm{mol})+(2 \mathrm{~mol})(0 \mathrm{~kJ} / \mathrm{mol})]=-656.988=-\mathbf{6 5 7 . 0} \mathbf{~ k J} } \\
& 2 \mathrm{SiO}_{2}(\mathrm{~s})+2 \mathrm{C}(\mathrm{graphite})+2 \mathrm{Cl}_{2}(\mathrm{~g}) \rightarrow \mathrm{SiCl}_{4}(\mathrm{~g})+2 \mathrm{CO}(\mathrm{~g}) \\
& \Delta H_{\mathrm{rxn}}^{\circ}=\left\{1 \Delta H_{\mathrm{f}}^{\circ}\left[\mathrm{SiCl}_{4}(\mathrm{~g})\right]+2 \Delta H_{\mathrm{f}}^{\circ}[\mathrm{CO}(\mathrm{~g})]\right\} \\
& \quad-\left\{1 \Delta H_{\mathrm{f}}^{\circ}\left[\mathrm{SiO}_{2}(\mathrm{~g})\right]+2 \Delta H_{\mathrm{f}}^{\circ}[\mathrm{C}(\text { graphite })]+2 \Delta H_{\mathrm{f}}^{\circ}\left[\mathrm{Cl}_{2}(\mathrm{~g})\right]\right\} \\
&= {[(1 \mathrm{~mol})(-656.988 \mathrm{~kJ} / \mathrm{mol})+(2 \mathrm{~mol})(-110.5 \mathrm{~kJ} / \mathrm{mol})] } \\
& \quad-[(1 \mathrm{~mol})(-910.9 \mathrm{~kJ} / \mathrm{mol})+(2 \mathrm{~mol})(0 \mathrm{~kJ} / \mathrm{mol})+(2 \mathrm{~mol})(0 \mathrm{~kJ} / \mathrm{mol})] \\
&= 32.912=\mathbf{3 2 . 9} \mathbf{~ k J}
\end{aligned}
$$

b) Adding reactions 2 and 3 yields:
(2) $\quad \mathrm{SiO}_{2}(\mathrm{~s})+2 \mathrm{C}($ graphite $)+2 \mathrm{Cl}_{2}(g) \rightarrow \mathrm{SiCl}_{4}(g)+2 \mathrm{CO}(g) \quad \Delta H_{\mathrm{rxn}}^{\circ}=32.912 \mathrm{~kJ}$
(3) $\quad \mathrm{SiCl}_{4}(g)+2 \mathrm{H}_{2} \mathrm{O}(g) \rightarrow \mathrm{SiO}_{2}(\mathrm{~s})+4 \mathrm{HCl}(g) \quad \Delta H_{\mathrm{rxn}}^{\circ}=-139.5 \mathrm{~kJ}$

2 C (graphite) $+2 \mathrm{Cl}_{2}(\mathrm{~g})+2 \mathrm{H}_{2} \mathrm{O}(\mathrm{g}) \rightarrow 2 \mathrm{CO}(\mathrm{g})+4 \mathrm{HCl}(\mathrm{g})$

$$
\Delta H_{\mathrm{rxn}}^{\circ}=-106.588 \mathrm{~kJ}=-\mathbf{1 0 6 . 6} \mathbf{~ k J}
$$

Confirm this result by calculating $\Delta H_{\mathrm{rxn}}^{\mathrm{o}}$ using Appendix B values.
2 C (graphite) $+2 \mathrm{Cl}_{2}(g)+2 \mathrm{H}_{2} \mathrm{O}(g) \rightarrow 2 \mathrm{CO}(g)+4 \mathrm{HCl}(g)$
$\Delta H_{\mathrm{rxn}}^{\circ}=\left\{2 \Delta H_{\mathrm{f}}^{\circ}[\mathrm{CO}(\mathrm{g})]+4 \Delta H_{\mathrm{f}}^{\circ}[\mathrm{HCl}(\mathrm{g})]\right\}-\left\{2 \Delta H_{\mathrm{f}}^{\circ}[\mathrm{C}(\right.$ graphite $\left.)]+2 \Delta H_{\mathrm{f}}^{\circ}\left[\mathrm{Cl}_{2}(\mathrm{~g})\right]+2 \Delta H_{\mathrm{f}}^{\circ}\left[\mathrm{H}_{2} \mathrm{O}(\mathrm{g})\right]\right\}$

$$
=[(2 \mathrm{~mol})(-110.5 \mathrm{~kJ} / \mathrm{mol})+(4 \mathrm{~mol})(-92.31 \mathrm{~kJ})
$$

$$
=-106.588=-\mathbf{1 0 6 . 6} \mathbf{k J}
$$

$$
-[(2 \mathrm{~mol})(0 \mathrm{~kJ} / \mathrm{mol})+(2 \mathrm{~mol})(0 \mathrm{~kJ} / \mathrm{mol})+(2 \mathrm{~mol})(-241.826 \mathrm{~kJ} / \mathrm{mol})]
$$

6.79 This is a Hess's Law problem. $\Delta H_{\mathrm{f}}^{\circ}$ of $\mathrm{HCl}\left[1 / 2 \mathrm{H}_{2}(g)+1 / 2 \mathrm{Cl}_{2}(g) \rightarrow \mathrm{HCl}(g)\right]$ must be found using the following equations:

1) $\mathrm{N}_{2}(g)+3 \mathrm{H}_{2}(g) \rightarrow 2 \mathrm{NH}_{3}(g)$
$\Delta H_{\mathrm{rxn}}^{\circ}=-91.8 \mathrm{~kJ}$
2) $\mathrm{N}_{2}(g)+4 \mathrm{H}_{2}(g)+\mathrm{Cl}_{2}(g) \rightarrow 2 \mathrm{NH}_{4} \mathrm{Cl}(\mathrm{s})$
$\Delta H_{\mathrm{rxn}}^{\circ}=-628.8 \mathrm{~kJ}$
3) $\mathrm{NH}_{3}(g)+\mathrm{HCl}(g) \rightarrow \mathrm{NH}_{4} \mathrm{Cl}(\mathrm{s})$
$\Delta H_{\mathrm{rxn}}^{\circ}=-176.2 \mathrm{~kJ}$

Reverse equation 1 and divide by 2 ; divide equation 2 by 2 ; finally, reverse equation 3 . This gives:

$$
\begin{array}{ll}
\text { 1) } \mathrm{NH}_{3}(g) \rightarrow 1 / 2 \mathrm{~N}_{2}(g)+3 / 2 \mathrm{H}_{2}(g) & \Delta H_{\mathrm{rxn}}^{\circ}=-1 / 2(-91.8 \mathrm{~kJ})=45.9 \mathrm{~kJ} \\
\text { 2) } \mathrm{A} / 2 \mathrm{~N}_{2}(g)+2 \mathrm{H}_{2}(g)+1 / 2 \mathrm{Cl}_{2}(g) \rightarrow \mathrm{NH}_{4} \mathrm{Cl}(\mathrm{~s}) & \Delta H_{\mathrm{rxn}}^{\circ}=1 / 2(-628.8 \mathrm{~kJ})=-314.4 \mathrm{~kJ} \\
\text { 3) } \mathrm{NH}_{4} \mathrm{Gl}(\mathrm{~s}) \rightarrow \mathrm{NH}_{3}(g)+\mathrm{HCl}(g) & \Delta H_{\mathrm{rxn}}^{\circ}=-(-176.2 \mathrm{~kJ})=176.2 \mathrm{~kJ}
\end{array}
$$

$$
1 / 2 \mathrm{H}_{2}(g)+1 / 2 \mathrm{Cl}_{2}(g) \rightarrow \mathrm{HCl}(g)
$$

a) $-q_{\mathrm{rxn}}=q_{\text {water }}+q_{\text {calorimeter }}$
$-q_{\mathrm{rxn}}=(50.0 \mathrm{~mL})\left(\frac{10^{-3} \mathrm{~L}}{1 \mathrm{~mL}}\right)\left(\frac{2.00 \mathrm{~mol}}{\mathrm{~L}}\right)\left(\frac{-57.32 \mathrm{~kJ}}{\mathrm{~mol}}\right)=5.732 \mathrm{~kJ}$
$q_{\text {water }}=($ mass $)(\mathrm{c})(\Delta \mathrm{T})$
$\left[100.0 \mathrm{~mL}\left(\frac{1.04 \mathrm{~g}}{\mathrm{~mL}}\right)\right]\left(3.93 \frac{\mathrm{~J}}{\mathrm{~g}^{\circ} \mathrm{C}}\right)\left((30.4-16.9)^{\circ} \mathrm{C}\right)\left(\frac{1 \mathrm{~kJ}}{10^{3} \mathrm{~J}}\right)=5.51772 \mathrm{~kJ}$
$q_{\text {calorimeter }}=q_{\mathrm{rxn}}-q_{\text {water }}=(5.732 \mathrm{~kJ})-(5.51772 \mathrm{~kJ})=0.21428 \mathrm{~kJ}$
$\mathrm{C}_{\text {calorimeter }}=q_{\text {calorimeter }} / \Delta \mathrm{T}=(0.21428 \mathrm{~kJ}) /(30.4-16.9)^{\circ} \mathrm{C}=0.01587=\mathbf{0 . 0 1 6} \mathbf{~ k J} /{ }^{\circ} \mathbf{C}$
b) Mole $\mathrm{HCl}=(100.0 \mathrm{~mL})\left(\frac{10^{-3} \mathrm{~L}}{1 \mathrm{~mL}}\right)\left(\frac{1.00 \mathrm{~mol} \mathrm{HCl}}{\mathrm{L}}\right)=0.100 \mathrm{~mol} \mathrm{HCl}$

Mole $\mathrm{Zn}=(1.3078 \mathrm{~g} \mathrm{Zn})\left(\frac{1 \mathrm{~mol} \mathrm{Zn}}{65.41 \mathrm{~g} \mathrm{Zn}}\right)=0.01999 \mathrm{~mol} \mathrm{Zn}$
Zn is the limiting reactant.
$-q_{\mathrm{rxn}}=q_{\text {water }}+q_{\text {calorimeter }}$ $=\left[100.0 \mathrm{~mL}\left(\frac{1.015 \mathrm{~g}}{\mathrm{~mL}}\right)+1.3078 \mathrm{~g}\right]\left(3.95 \frac{\mathrm{~J}}{\mathrm{~g}^{\circ} \mathrm{C}}\right)\left((24.1-16.8)^{\circ} \mathrm{C}\right)\left(\frac{1 \mathrm{~kJ}}{10^{3} \mathrm{~J}}\right)+\left(0.01587 \frac{\mathrm{~kJ}}{{ }^{\circ} \mathrm{C}}\right)\left((24.1-16.8)^{\circ} \mathrm{C}\right)$

$$
=3.0803 \mathrm{~kJ}
$$

$\Delta H_{\mathrm{rxn}}^{\circ}=(-3.0803 \mathrm{~kJ}) /(0.01999 \mathrm{~mol} \mathrm{Zn})=-154.1=\mathbf{- 1 . 5 \times 1 0 ^ { 2 }} \mathbf{~ k J} / \mathbf{m o l}$
c) $\mathrm{Zn}(s)+2 \mathrm{HCl}(a q) \rightarrow \mathrm{ZnCl}_{2}(a q)+\mathrm{H}_{2}(g)$
$\Delta H_{\mathrm{rxn}}^{\circ}=\left\{1 \Delta H_{\mathrm{f}}^{\circ}\left[\mathrm{ZnCl}_{2}(a q)\right]+1\left[\Delta H_{\mathrm{f}}^{\circ} \mathrm{H}_{2}(g)\right]\right\}-\left\{1 \Delta H_{\mathrm{f}}^{\circ}[\mathrm{Zn}(s)]+2 \Delta H_{\mathrm{f}}^{\circ}[\mathrm{HCl}(a q)]\right\}$
$\Delta H_{\mathrm{rxn}}^{\circ}=\left[(1 \mathrm{~mol})\left(-4.822 \times 10^{2} \mathrm{~kJ} / \mathrm{mol}\right)+(1 \mathrm{~mol})(0.0 \mathrm{~kJ} / \mathrm{mol})\right]$ $-\left[(1 \mathrm{~mol})(0.0 \mathrm{~kJ} / \mathrm{mol})+(2 \mathrm{~mol})\left(-1.652 \times 10^{2} \mathrm{~kJ} / \mathrm{mol}\right)\right]$
$\Delta H_{\mathrm{rxn}}^{\circ}=-151.8 \mathrm{~kJ}$

$$
\text { Error }=\left|\frac{-151.8-(-154.1)}{-151.8}\right|(100 \%)=1.515=2 \%
$$

Plan: Use $P V=n R T$ to find the initial volume of nitrogen gas at $0^{\circ} \mathrm{C}$ and then the final volume at $819^{\circ} \mathrm{C}$. Then the relationship $w=-P \Delta V$ can be used to calculate the work of expansion.

Solution:
a) $P V=n R T$

Initial volume at $0^{\circ} \mathrm{C}+273=273 \mathrm{~K}=V=\frac{n R T}{P}=\frac{(1 \mathrm{~mol})\left(0.0821 \frac{\mathrm{~L} \cdot \mathrm{~atm}}{\mathrm{~mol} \cdot \mathrm{~K}}\right)(273 \mathrm{~K})}{(1.00 \mathrm{~atm})}=22.4133 \mathrm{~L}$
Final volume at $819^{\circ} \mathrm{C}+273=1092 \mathrm{~K}=V=\frac{n R T}{P}=\frac{(1 \mathrm{~mol})\left(0.0821 \frac{\mathrm{~L} \cdot \mathrm{~atm}}{\mathrm{~mol} \cdot \mathrm{~K}}\right)(1092 \mathrm{~K})}{(1.00 \mathrm{~atm})}=89.6532 \mathrm{~L}$
$\Delta V=V_{\text {final }}-V_{\text {initial }}=89.6532 \mathrm{~L}-22.4133 \mathrm{~L}=67.2399 \mathrm{~L}$
$w=-P \Delta V=-(1 \mathrm{~atm}) \times 67.2399 \mathrm{~L}=-67.2399 \mathrm{~atm} \cdot \mathrm{~L}$
$w(\mathrm{~J})=(-67.2399 \mathrm{~atm} \cdot \mathrm{~L})\left(\frac{1 \mathrm{~J}}{9.87 \times 10^{-3} \mathrm{~atm} \cdot \mathrm{~L}}\right)=-6812.553=-\mathbf{6 . 8 1 \times 1 0 ^ { 3 }} \mathbf{J}$
b) $q=c \times$ mass $\times \Delta T$

Mass $(\mathrm{g})$ of $\mathrm{N}_{2}=\left(1 \mathrm{~mol} \mathrm{~N}_{2}\right)\left(\frac{28.02 \mathrm{~g}}{1 \mathrm{~mol} \mathrm{~N}_{2}}\right)=28.02 \mathrm{~g}$

$$
\Delta T=\frac{q}{(c)(\mathrm{mass})}=\frac{6.812553 \times 10^{3} \mathrm{~J}}{(28.02 \mathrm{~g})(1.00 \mathrm{~J} / \mathrm{g} \cdot \mathrm{~K})}=243.132=243 \mathrm{~K}=243^{\circ} \mathrm{C}
$$

Multiply (3) by 2
(5)

Plan: Note the numbers of moles of the reactants and products in the target equation and manipulate equations 1-5 and their $\Delta H_{\mathrm{rxn}}^{\circ}$ values so that these equations sum to give the target equation. Then the manipulated $\Delta H_{\mathrm{rxn}}^{\mathrm{o}}$ values will add to give the $\Delta H_{\mathrm{rxn}}^{\circ}$ value of the target equation.

## Solution:

Only reaction 3 contains $\mathrm{N}_{2} \mathrm{O}_{4}(\mathrm{~g})$, and only reaction 1 contains $\mathrm{N}_{2} \mathrm{O}_{3}(\mathrm{~g})$, so we can use those reactions as a starting point. $\mathrm{N}_{2} \mathrm{O}_{5}$ appears in both reactions 2 and 5, but note the physical states present: solid and gas. As a rough start, adding reactions 1,3 , and 5 yields the desired reactants and products, with some undesired intermediates:

Reverse (1) $\quad \mathrm{N}_{2} \mathrm{O}_{3}(g) \quad \rightarrow \mathrm{NO}(g)+\mathrm{NO}_{2}(g) \quad \Delta H_{\mathrm{rxn}}^{\circ}=-(-39.8 \mathrm{~kJ})=39.8$

$$
\mathrm{N}_{2} \mathrm{O}_{3}(g)+4 \mathrm{NO}_{2}(g)+\mathrm{N}_{2} \mathrm{O}_{5}(s) \rightarrow \mathrm{NO}(g)+\mathrm{NO}_{2}(g)+2 \mathrm{~N}_{2} \mathrm{O}_{4}(g)+\mathrm{N}_{2} \mathrm{O}_{5}(g)
$$

To cancel out the $\mathrm{N}_{2} \mathrm{O}_{5}(g)$ intermediate, reverse equation 2. This also cancels out some of the undesired $\mathrm{NO}_{2}(g)$ but adds $\mathrm{NO}(\mathrm{g})$ and $\mathrm{O}_{2}(\mathrm{~g})$. Finally, add equation 4 to remove those intermediates:

| Reverse (1) | $\mathrm{N}_{2} \mathrm{O}_{3}(g) \rightarrow \mathrm{NO}(g)+\mathrm{NO}_{2}(g)$ | $\Delta H_{\mathrm{rxn}}^{\circ}=-(-39.8 \mathrm{~kJ})=$ | 39.8 kJ |
| :--- | :--- | :--- | :--- |
| Multiply (3) by 2 | $4 \mathrm{NO}_{2}(g) \rightarrow 2 \mathrm{~N}_{2} \mathrm{O}_{4}(g)$ | $\Delta H_{\mathrm{rxn}}^{\circ}=2(-57.2 \mathrm{~kJ})=-114.4 \mathrm{~kJ}$ |  |
| (5) | $\mathrm{N}_{2} \mathrm{O}_{5}(\mathrm{~s}) \rightarrow \mathrm{N}_{2} \mathrm{O}_{5}(g)$ | $\Delta H_{\mathrm{rxn}}^{\circ}=$ | 54.1 kJ |
| Reverse (2) | $\mathrm{N}_{2} \Theta_{5}(g) \rightarrow \mathrm{NO}(g)+\mathrm{NO}_{z}(g)+\mathrm{O}_{z}(g)$ | $\Delta H_{\mathrm{rxn}}^{\circ}=-(-112.5 \mathrm{~kJ})=112.5$ |  |
| (4) | $2 \mathrm{NO}(g)+\mathrm{O}_{2}(g) \rightarrow 2 \mathrm{NO}_{2}(g)$ | $\Delta H_{\mathrm{rxn}}^{\circ}=$ | -114.2 kJ |
| Total: | $\mathrm{N}_{2} \mathrm{O}_{3}(g)+\mathrm{N}_{2} \mathrm{O}_{5}(\mathrm{~s}) \rightarrow 2 \mathrm{~N}_{2} \mathrm{O}_{4}(g)$ | $\Delta H_{\mathrm{rxn}}^{\circ}=$ | $\mathbf{- 2 2 . 2 ~ k J}$ |

```
\(\mathrm{CO}(\mathrm{g})+2 \mathrm{H}_{2}(\mathrm{~g}) \rightarrow \mathrm{CH}_{3} \mathrm{OH}(\mathrm{l})\)
\(\Delta H_{\mathrm{rxn}}^{\circ}=\left\{1 \Delta H_{\mathrm{f}}^{\circ}\left[\mathrm{CH}_{3} \mathrm{OH}(\mathrm{l})\right]\right\}-\left\{1 \Delta H_{\mathrm{f}}^{\circ}[\mathrm{CO}(\mathrm{g})]+2 \Delta H_{\mathrm{f}}^{\circ}\left[\mathrm{H}_{2}(\mathrm{~g})\right]\right\}\)
    \(=[(1 \mathrm{~mol})(-238.6 \mathrm{~kJ} / \mathrm{mol})]-[(1 \mathrm{~mol})(-110.5 \mathrm{~kJ} \mathrm{~mol})+(2 \mathrm{~mol})(0.0 \mathrm{~kJ} / \mathrm{mol})]\)
    \(=-128.1 \mathrm{~kJ}\)
```

Find the limiting reactant:
Moles of $\mathrm{CO}=\frac{P V}{R T}=\frac{(112 \mathrm{kPa})(15.0 \mathrm{~L})}{\left(0.0821 \frac{\mathrm{~L} \cdot \mathrm{~atm}}{\mathrm{~mol} \cdot \mathrm{~K}}\right)((273+85) \mathrm{K})}\left(\frac{1 \mathrm{~atm}}{101.325 \mathrm{kPa}}\right)=0.5641135 \mathrm{~mol} \mathrm{CO}$
Moles of $\mathrm{CH}_{3} \mathrm{OH}$ from $\mathrm{CO}=(0.5641135 \mathrm{~mol} \mathrm{CO})\left(\frac{1 \mathrm{~mol} \mathrm{CH}_{3} \mathrm{OH}}{1 \mathrm{~mol} \mathrm{CO}}\right)=0.5641135 \mathrm{~mol} \mathrm{CH}_{3} \mathrm{OH}$
Moles of $\mathrm{H}_{2}=\frac{P V}{R T}=\frac{(744 \mathrm{torr})(18.5 \mathrm{~L})}{\left(0.0821 \frac{\mathrm{~L} \cdot \mathrm{~atm}}{\mathrm{~mol} \cdot \mathrm{~K}}\right)((273+75) \mathrm{K})}\left(\frac{1 \mathrm{~atm}}{760 \mathrm{torr}}\right)=0.6338824 \mathrm{~mol} \mathrm{H}_{2}$
Moles of $\mathrm{CH}_{3} \mathrm{OH}$ from $\mathrm{H}_{2}=\left(0.6338824 \mathrm{~mol} \mathrm{H}_{2}\right)\left(\frac{1 \mathrm{~mol} \mathrm{CH}_{3} \mathrm{OH}}{2 \mathrm{~mol} \mathrm{H}_{2}}\right)=0.3169412 \mathrm{~mol} \mathrm{CH}_{3} \mathrm{OH}$
$\mathrm{H}_{2}$ is limiting.
Heat $(\mathrm{kJ})=\left(0.6338824 \mathrm{~mol} \mathrm{H}_{2}\right)\left(\frac{-128.1 \mathrm{~kJ}}{2 \mathrm{~mol} \mathrm{H}_{2}}\right)=-40.6002=-\mathbf{4 0 . 6} \mathbf{~ k J}$
6.84 Plan: First find the heat of reaction for the combustion of methane. The enthalpy change of a reaction is the sum of the heats of formation of the products minus the sum of the heats of formation of the reactants. Since the
$\Delta H_{\mathrm{f}}^{\circ}$ values (Appendix B) are reported as energy per one mole, use the appropriate stoichiometric coefficient to reflect the higher number of moles. Convert the mass of methane to moles and multiply that mole number by the heat of combustion.
Solution:
a) The balanced chemical equation for this reaction is:

$$
\begin{aligned}
\mathrm{CH}_{4}(g) & +2 \mathrm{O}_{2}(g) \rightarrow \mathrm{CO}_{2}(g)+2 \mathrm{H}_{2} \mathrm{O}(g) \\
\Delta H_{\mathrm{rxn}}^{\circ} & =\left\{1 \Delta H_{\mathrm{f}}^{\circ}\left[\mathrm{CO}_{2}(g)\right]+2 \Delta H_{\mathrm{f}}^{\circ}\left[\mathrm{H}_{2} \mathrm{O}(g)\right]\right\}-\left\{1 \Delta H_{\mathrm{f}}^{\circ}\left[\mathrm{CH}_{4}(g)\right]+2 \Delta H_{\mathrm{f}}^{\circ}\left[\mathrm{O}_{2}(g)\right]\right\} \\
& =[(1 \mathrm{~mol})(-393.5 \mathrm{~kJ} / \mathrm{mol})+(2 \mathrm{~mol})(-241.826 \mathrm{~kJ} / \mathrm{mol})]-[(1 \mathrm{~mol})(-74.87 \mathrm{~kJ} / \mathrm{mol})+(2 \mathrm{~mol})(0.0 \mathrm{~kJ} / \mathrm{mol})] \\
& =-802.282 \mathrm{~kJ}
\end{aligned}
$$

Moles of $\mathrm{CH}_{4}=\left(25.0 \mathrm{~g} \mathrm{CH}_{4}\right)\left(\frac{1 \mathrm{~mol}}{16.04 \mathrm{~g} \mathrm{CH}_{4}}\right)=1.5586 \mathrm{~mol} \mathrm{CH}_{4}$
Heat $(\mathrm{kJ})=\left(1.5586 \mathrm{~mol} \mathrm{CH}_{4}\right)\left(\frac{-802.282 \mathrm{~kJ}}{1 \mathrm{~mol} \mathrm{CH}_{4}}\right)=-1250.4=\mathbf{- 1 . 2 5 \times 1 0 ^ { \mathbf { 3 } } \mathbf { ~ k J }}$
b) The heat released by the reaction is "stored" in the gaseous molecules by virtue of their specific heat capacities, $c$, using the equation $q=c \times$ mass $\times \Delta T$. The problem specifies heat capacities on a molar basis, so we modify the equation to use moles, instead of mass. The gases that remain at the end of the reaction are $\mathrm{CO}_{2}$ and $\mathrm{H}_{2} \mathrm{O}$. All of the methane and oxygen molecules were consumed. However, the oxygen was added as a component of air, which is $78 \% \mathrm{~N}_{2}$ and $21 \% \mathrm{O}_{2}$, and there is leftover $\mathrm{N}_{2}$.
Moles of $\mathrm{CO}_{2}(g)=\left(1.5586 \mathrm{~mol} \mathrm{CH}_{4}\right)\left(\frac{1 \mathrm{~mol} \mathrm{CO}_{2}}{1 \mathrm{~mol} \mathrm{CH}_{4}}\right)=1.5586 \mathrm{~mol} \mathrm{CO}_{2}(g)$
Moles of $\mathrm{H}_{2} \mathrm{O}(\mathrm{g})=\left(1.5586 \mathrm{~mol} \mathrm{CH}_{4}\right)\left(\frac{2 \mathrm{~mol} \mathrm{H}_{2} \mathrm{O}}{1 \mathrm{~mol} \mathrm{CH}_{4}}\right)=3.1172 \mathrm{~mol} \mathrm{H}_{2} \mathrm{O}(g)$
Moles of $\mathrm{O}_{2}(\mathrm{~g})$ reacted $=(1.5586 \mathrm{~mol} \mathrm{CH} 44)\left(\frac{2 \mathrm{~mol} \mathrm{O}_{2}}{1 \mathrm{~mol} \mathrm{CH}_{4}}\right)=3.1172 \mathrm{~mol} \mathrm{O}_{2}(\mathrm{~g})$
Mole fraction $\mathrm{N}_{2}=(79 \% / 100 \%)=0.79$
Mole fraction $\mathrm{O}_{2}=(21 \% / 100 \%)=0.21$
Moles of $\mathrm{N}_{2}(g)=\left(3.1172 \mathrm{~mol} \mathrm{O} \mathrm{O}_{2}\right.$ reacted $)\left(\frac{0.79 \mathrm{~mol} \mathrm{~N}_{2}}{0.21 \mathrm{~mol} \mathrm{O}_{2}}\right)=11.72661 \mathrm{~mol} \mathrm{~N}_{2}$

$$
\begin{aligned}
& q=c \times \text { mass } \times \Delta T \\
& q=(1250.4 \mathrm{~kJ})\left(\frac{10^{3} \mathrm{~J}}{1 \mathrm{~kJ}}\right)=1.2504 \times 10^{6} \mathrm{~J} \\
& 1.2504 \times 10^{6} \mathrm{~J}=(1.5586 \mathrm{~mol} \mathrm{CO} 2)\left(57.2 \mathrm{~J} / \mathrm{mol}^{\circ} \mathrm{C}\right)\left(T_{\text {final }}-0.0\right)^{\circ} \mathrm{C} \\
& +\left(3.1172 \mathrm{~mol} \mathrm{H} \mathrm{H}_{2} \mathrm{O}\right)\left(36.0 \mathrm{~J} / \mathrm{mol}^{\circ} \mathrm{C}\right)\left(T_{\text {final }}-0.0\right)^{\circ} \mathrm{C} \\
& +\left(11.72661 \mathrm{~mol} \mathrm{~N}_{2}\right)\left(30.5 \mathrm{~J} / \mathrm{mol}^{\circ} \mathrm{C}\right)\left(T_{\text {final }}-0.0\right)^{\circ} \mathrm{C} \\
& 1.2504 \times 10^{6} \mathrm{~J}=89.15192 \mathrm{~J} /{ }^{\circ} \mathrm{C}\left(T_{\text {final }}\right)+112.2192 \mathrm{~J} /{ }^{\circ} \mathrm{C}\left(T_{\text {final }}\right)+357.6616 \mathrm{~J} /{ }^{\circ} \mathrm{C}\left(T_{\text {final }}\right) \\
& 1.2504 \times 10^{6} \mathrm{~J}=\left(559.03272 \mathrm{~J} /{ }^{\circ} \mathrm{C}\right) T_{\text {final }} \\
& T_{\text {final }}=\left(1.2504 \times 10^{6} \mathrm{~J}\right) /\left(559.0324 \mathrm{~J} /{ }^{\circ} \mathrm{C}\right)=2236.72=\mathbf{2 . 2 4 \times 1 0 ^ { 3 }}{ }^{\circ} \mathrm{C}
\end{aligned}
$$

